

**Optimal design of seismic retrofitting by
means of viscous dampers:
A quantitative comparison**

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