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Scuola di Ingegneria Industriale e dell'Informazione

Corso di Laurea Magistrale in Ingegneria Informatica

Dipartimento di Elettronica, Informazione e Bioingegneria



Inferenza di Reti di Interazioni Diadiche da Dati Sensoriali

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Anno Accademico 2015-2016

*To my uncle Gianni, my memory of you will always inspire me to achieve all my goals in life,
just as you did.*

ACKNOWLEDGMENTS

I would like to thank my parents, Adriana and Marcello, who made this dream come true, and my brother Nestore, who has always been there for me when I needed.

I believe both Politecnico di Milano and University of Illinois at Chicago formed me the way I am now, and I am really grateful for that. In particular I would like to thank Tanya Berger-Wolf, Pier Luca Lanzi and Robert Kenyon who also helped me with my mental growth, doing and caring about me much more than what is usually expected from a professor.

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LIST OF ABBREVIATIONS

GPS	Global Positioning System
DNA	Deoxyribonucleic Acid
WAAS	Wide Area Augmentation System
BLE	Bluetooth Low Energy
RSSI	Received Signal Strength Indication
SVM	Support Vector Machine
NN	Neural Network
MPU	Magnetic Pick-Up
FSM	Finite-State Machine
ReLU	Rectified Linear Unit
OFAT	One-Factor-At-a-Time
DT	Decision Tree

ABSTRACT

Being able to observe how animals interact among themselves has always been a crucial requirement for behavioral scientists who study social species. Manually looking at them to see when interactions occur is extremely time-consuming, results in many missing observations and it becomes extremely difficult to do for a very extended period of time, moreover for animals who live in large territories and for animals who behave differently when nearby human beings. To overcome these problems, scientists are accustomed to use several different kinds of sensors which are usually attached to the target animals and record some kind of raw data which, once collected, is used to extract the behavior of their hosts.

These sensors have to be as least invasive as possible for the animal to behave as if it wasn't wearing them. This implies that sensors have to be light with respect to the animal, they must not emit a considerable amount of heat and the wavelength they use must not be perceptible by the animals near them.

The most popular type of data extracted from sensors attached to animals is Global Positioning System (GPS) data. GPS data is very easy to extract and it can be used to efficiently track the positions of entire groups of animals. However, when we are interested in pairwise interactions between animals and not in their positions, GPS data is not very reliable either because of its accuracy and because of its reliability.

In this work, we introduce synthesized sensor data based on a type of non-invasive short range proximity sensors in order to understand whether some animals interact among themselves

ABSTRACT (continued)

at a given time. The data we consider has to be labeled, that is we are aware of most interactions that occur during the training phase.

The sensors whose data we are interested in synthesizing can be used for animals that are capable of wearing them due to weight or size constraints and as long as the sensor range contains the interaction range of the animals we are interested in. The models we analyze in this work are of two types: those which don't assume either equality of the individuals and independence among interactions, and those which assume both of them.

We present a framework to synthesize proximity, location and speed data extracted from sensors with several different configurations and models to infer animal interactions.

Finally, we evaluate the methodology we use by proposing a case study where we perform different analyses to understand when our models are fit for the inference task, what are the most critical parameters impacting their performances and when we should switch from a model with no assumption to one with the two previously mentioned.

SOMMARIO

Essere in grado di osservare come gli animali interagiscono tra di loro è sempre stato un requisito fondamentale per gli etologi. Guardarli manualmente per vedere quando si verificano interazioni richiede un notevole spreco di tempo, risultante peraltro in molte osservazioni mancate, e diventa estremamente difficile da fare per un periodo molto prolungato di tempo, in particolare per animali che vivono in ampi territori e per animali che si comportano in modo diverso con umani nelle vicinanze. Per superare questi problemi, gli scienziati sono abituati a utilizzare diversi tipi di sensori che sono solitamente collegati agli animali interessati per registrare qualche tipo di dati grezzo che, una volta raccolto, viene utilizzato per estrarre il comportamento dei loro ospiti.

Questi sensori devono essere il meno invasivi possibile per indurre l'animale a comportarsi come se non li indossasse. Ciò implica che i sensori devono essere leggeri rispetto all'animale, non devono emettere una notevole quantità di calore e la lunghezza d'onda che usano non deve essere percepibile dagli animali vicino a loro.

Il tipo più popolare di dati estratti da sensori collegati agli animali è GPS. I dati GPS sono molto facili da estrarre e possono essere utilizzati per monitorare efficacemente le posizioni di interi gruppi di animali. Tuttavia, quando siamo interessati a interazioni diadiche (a coppie) tra gli animali e non alle loro posizioni, i dati GPS non sono ideali sia a causa della loro precisione sia per la loro affidabilità.

SOMMARIO (continued)

In questo lavoro, introduciamo dei dati sintetizzati basandoci su un tipo di sensori a corto raggio di prossimità non invasivi per capire se alcuni animali interagiscono tra loro in un dato momento. I dati che consideriamo devono essere etichettati, cioè siamo a conoscenza della maggior parte delle interazioni che si verificano durante la fase di addestramento dei nostri modelli.

I sensori dei quali dati siamo interessati a sintetizzare possono essere utilizzati con animali che sono capaci di indossarli, condizionati dal volume e peso di entrambi e finchè la portata dei sensori comprende la portata delle interazioni degli animali di cui siamo interessati. I modelli che analizziamo in questo lavoro sono di due tipi: quelli che non assumono nè uguaglianza degli individui nè indipendenza tra interazioni, e quelle che le assumono entrambe.

Presentiamo un framework per sintetizzare dati di prossimità, posizione e velocità estratti da sensori con diverse configurazioni e modelli per dedurre le interazioni diadiche degli animali.

Infine, valutiamo la metodologia che usiamo proponendo un caso di studio in cui eseguiamo diverse analisi per capire quando i nostri modelli sono idonei per il compito, quali sono i parametri più critici che incidono sulle loro prestazioni e quando dovremmo passare da un modello senza assunzioni ad uno con le due precedentemente accennate.

CHAPTER 1

INTRODUCTION

Humans have been observing animals since ancient times. The reasons have been very different: from being as effective as possible for hunting and to avoid dangerous predators to pure interest in their everyday life.

After the work of Charles Darwin and the birth of the theory of Evolution [1], observing animals has become extremely interesting because of the connection of animals with humans. Moreover, with the discovery of the Deoxyribonucleic Acid (DNA) in 1869 and its molecular structure's identification in 1953 [2], the study of animal behavior has become important to also understand human behavior.

However, observing animals is not always an easy task, either because of the time it takes to gather significant information from them and because sometimes it is very hard to follow some types of animals, such as predators whose territory is usually very vast. The advent of the technology revolution of the most recent years gave biologists a new way to observe animals.

By exploiting sensors attached to several individuals of a given species, we can observe their movements for a very long period of time. This gives us insight of what certain animals do, where they go, what is their usual route, for example for hunting, and ultimately how they interact with their environment and companions even when it wouldn't be possible to be observed by a scientist.

The most used sensor data for these tasks nowadays is GPS data. It is a space-based navigation system which gives information about time and position, given in longitude and latitude, and can be used anywhere in the world as long as there are four or more GPS satellites that have an unobstructed line of sight to the sensor used. This makes GPS data available almost anywhere on Earth and extremely efficient in tracking the movements of animals in their habitat, especially when they live in a vast area free of obstructions, basically anywhere but thick forests.

However, GPS data has its shortcomings: the standard accuracy of an average GPS sensor is about 15 meters (49 feet), which can be improved to 3 meters (9.8 feet) by using Wide Area Augmentation System (WAAS). The accuracy of a sensor is how confident we are about the position we are recording. This means that having an accuracy of 3 meters implies that the real position of the sensor can be anywhere in a circle with a radius of 3 meters. Despite being acceptable for tracking animal movements in large areas, it is not the case when we want to spot interactions between two individuals.

In fact, animals tend to have topological interactions instead of metric interactions [3], that is they usually interact with a small, hardly varying number of closest animals instead of every animal closer than a threshold. Thus, being uncertain of a distance by four times the accuracy of a single sensor between two animals (twice the accuracy per animal), makes GPS data by itself, without great redundancy, unfit for the task of inferring dyadic interactions. Moreover, for smaller animals, the redundancy needed to have usable data might make the task impossible for weight as well as cost constraints.

An alternative to GPS data is to use Bluetooth Low Energy (BLE) transmitters and receivers so that the receiver is able to compute a Received Signal Strength Indication (RSSI) value, which stands for the strength of the signal between the two sensors. This is far more accurate than GPS data, however it does not give either absolute positions and always accurate absolute distances between sensors, because of the many reasons a signal could be weaker than expected. Still, it is sufficient when we want to understand interactions between animals, which is very dependent on their relative distances.

1.1 Thesis Models

This work will synthesize RSSI and accelerometer data to extract interactions among groups of animals. We will work with different configurations of sensors, creating a framework able to synthesize such arrangements to extract the best model for a given instance and test its performances with different parameters to understand when it does and does not perform well.

When scientists are interested in interactions between animals, what they *mean* for interaction may well vary from one to another. Some might consider an interaction when two animals are sufficiently near one another, others when one approaches the other and the interaction might be only an instant despite them being close for a longer period. Others might think an interaction is when two animals do something together, others when one follows another one. Being the word “interaction” so arbitrary, in order to train any model to fit the specific definition of any given instance, it implies the need to have *labeled* data.

Labeled data means that along with the raw input data which comes from the sensors, we are given the interactions that occur among the animals we are considering at any given time

period we are interested to sample. This is necessary for most models that want to learn how to predict an output, in our case the interactions between our animals, given an input, that is our raw data collected from sensors.

Unfortunately, this means that scientists still have to manually annotate interactions of animals for a fairly big amount of time: the longer they annotate interactions, the more robust the models will be. This might seem counter intuitive: we want to build a model to *not* manually annotate interactions, and we require them for our model to work. However, the *amount* of data we have to label is significantly different: ideally, once we labeled a sufficient amount of data, we would not need to label it anymore in the future, regardless of the number of instances we would be able to sample with our sensors. Suppose we had a month of recordings of interactions of animals, we would probably need to label only about a few days or even a few hours of interactions to be able to build a reasonably good model, which would then label all the remaining time.

The models we analyze in this work can be divided in two categories: the first category takes into account that each animal is different from every other, and if an interaction occurs between two animals, it may impact the likelihood of other interactions. These are probably some of the most non constraining assumptions we can make, however they have their shortcomings: they require *a lot* of data, w.r.t. other possibilities. Alternatively, we can create a model that doesn't take into account diversity of individuals and different likelihood of interactions given other interactions. These would usually perform well with far less data than what would be required by other models, but they may be less performing with more data.

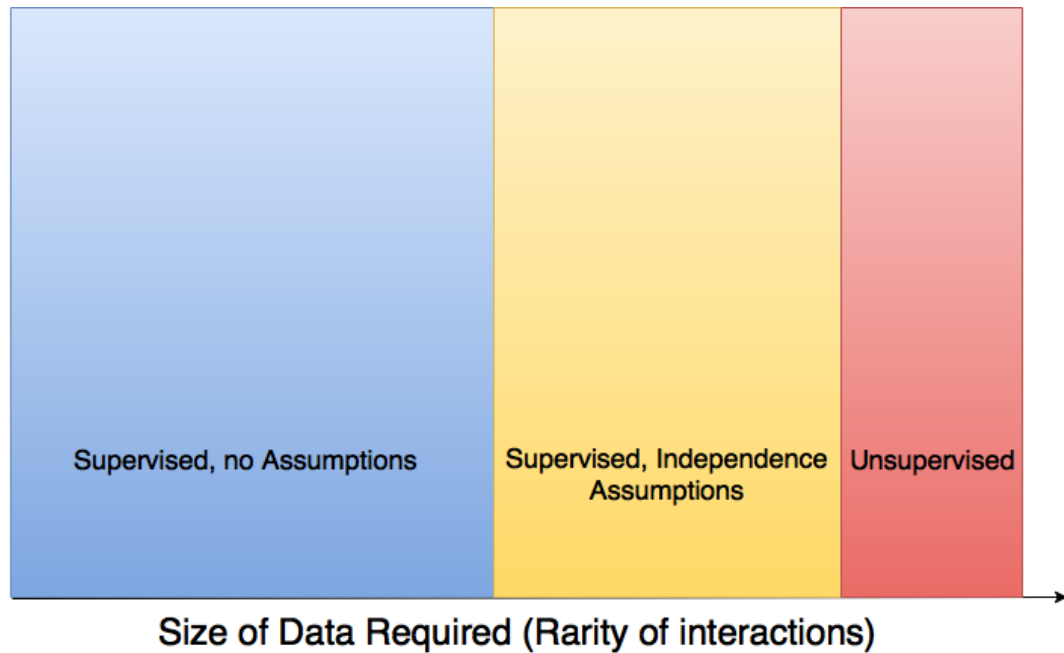


Figure 1: Partitioning of the best model to infer interactions with respect to the rarity of them.

We estimate that what is the ideal model to spot interactions depends on the rarity of the interactions themselves (Figure 1): when we have enough data to spot every single possible pairwise interaction a fair amount of times, we expect our first type of models to perform extremely well. However, when interactions become extremely rare and we only see a bunch of them, and not for every possible pair (which of course scales also with respect to the number of animals), we would need to drop some assumptions so that every label can be used to train *any* pairwise prediction.

Finally, when spotting interactions becomes extremely time consuming, we can decide to automatically detect them without training any model. This is called unsupervised learning,

and it should be used only when no other options are possible, because it is most likely going to give either an extremely big number of false positives or an extremely big number of false negatives, and the worst part of it is that, even if we can reason about the quantity of false positives, we *cannot* do so for false negatives: we wouldn't know how many interactions we are missing unless we started to manually label all our data.

1.2 Thesis Objective

This work is a direct extension of our previous work [4], by introducing a new family of classifiers and comparing them with the previously analyzed one. The goal of this thesis is twofold: we want to build some models to infer dyadic interactions given sensor data *before* actually deploying these sensors, in particular we want to be able to find the best model for any given instance following some guidelines, and we want to build a framework able to synthesize such data.

Deploying sensors is extremely costly, and biologists would like to know what sensors they need, how many and where to put them before actually building or buying them, and they would like to have assurances that once they collect some data, they can actually figure something out of it. This makes not only necessary to create a model beforehand, but it also requires it to be tested in a synthetic environment not too specific but not completely random, so not to be too biased, to be able to give some idea on the performances that it could have, and more importantly what types of sensors and what specifications they should have and what is more or less important (such as, with these sensors it seems to be able to learn, or, adding these sensors doesn't improve anything).

1.3 Structure of the Thesis

Chapter 2 will briefly give an insight of the related work. Interestingly enough, supervised learning has hardly ever been considered for animal interactions, most likely because of the time it would need to be done well. Chapter 3 will give necessary background of most of the approaches we will use to build our framework. This chapter is intended to aid a lack of knowledge in a specific area and it is not necessary whenever the reader has already a sufficiently large background on a specific subsection. We still recommend to quickly look at it even in the latter case, to better understand how we are going to use such concepts later on. Chapter 4 will explain the proposed approach. First, it will formally define our tasks, specifying our sensors and our configurations, second, it will explain our models and framework. Chapter 5 will show a case study where we will perform some sensitivity analysis and discuss the obtained results. Chapter 6 will give conclusive observations and talk about possible future work.

CHAPTER 2

RELATED WORK

Whenever we are interested in animals, we are interested in their behavior. Behavior is what makes an animal different from another, behavior is what leads an animal to do what they do. Whenever biologists are interested in studying animal behavior, they need to observe their behavior not only considering single individuals, but how they interact among themselves as well.

Although observing animals manually can be done [5; 6], it can only be done for a small amount of time and usually within small areas.

When interested in small animals constrained to live in a controlled environment such as fish or insects, video tracking technology can seriously help biologists [7; 8; 9].

When facing larger animals, we can sense various information such as their location, movement and orientation thanks to different wireless sensors [10; 11; 12; 13; 14; 15].

GPS data is customary to be used to track animal positions, a well known example is where researchers at Princeton built ZebraNet [16], a tracking system which involves the usage of tracking collars worn by some zebras in Kenya which collect GPS data. Tracking collars were also used to track deer movements over a seven-year time period [17].

However, GPS data is not accurate enough to be successfully used to spot animal interactions [18].

Video or RFID [19] can be used to better detect proximity among animals when it is possible to cover vast areas with location systems. However, it is hardly the case. Ultrasonic tracking could still be used for some animals [20], but it may disturb several other species, making it impossible to be deployed in most cases.

Regarding inferring animal interactions, researchers recently exploited GPS data to track baboons movements [21] in order to study shared decision making movements, dominance interactions by first automatically extracting and then manually validating them as well as extracting dominance hierarchies.

Scientists used k-means algorithm to cluster cows GPS data to spot different behaviors [22]. This is again an unsupervised learning classification. It is indeed usual to automatically extract interactions among animals in many different ways: unsupervised learning can be used to find interactions among cattle using a distance threshold and discern stronger ones by timing their lengths [23], scientists can exploit maximum entropy models to infer interactions of mice [24]; others [25] uses various formulas as well, but tested its results with some synthesized labeled data, and with a little real labeled data, also showing the usefulness of synthesizing this type of data.

However, unsupervised learning methods have various limitations despite being easy to deploy: inferring a specific kind of interaction is extremely difficult, in fact the interaction is defined by our model, there is no way to estimate its recall and a recent work [26] discusses how generally wrong is the concept of interaction extracted from thresholds w.r.t. what biologists really look for. An alternative to that is supervised learning, as shown another recent work [27],

where mouse social behaviors were extracted through a supervised learning approach involving data acquisition and adjustment from different sources and a labeling of around 150,000 video frames fed into a Random Decision Forest model.

The gain of supervised learning approaches is undeniable, thus in this work we are especially interested in knowing when we can exploit such a powerful method, instead of using the well known unsupervised approaches.

CHAPTER 3

BACKGROUND

This chapter is going to focus on giving a background knowledge of some key concepts which are going to be used in our proposed approach. Section 3.1 presents the concept of graphs. Section 3.2 explains the basic data subdivision used in building a model. Section 3.3 describes the Markov Assumption. Section 3.5 explains the concept of Support Vector Machine (SVM). Section 3.6 presents the model of Neural Network (NN) and the instances used in this work. Section 3.7 talks about Decision Tree (DT)s while focusing on its ensemble methods. Section 3.8 explains what is a test for statistical significance and why it is useful. Finally, Section 3.9 talks about Sensitivity Analysis, which is going to be the focus of our work.

3.1 Graph Representation

A graph is a mathematical representation of a set of objects usually referred to as vertices, nodes or points, where some pairs of them are connected by links, usually referred to as edges, arcs or lines. The links can either be directed, being referred as *arcs*, or undirected, usually being referred as *edges*. In our work we mostly name the objects *nodes* and the links *edges* when referring to undirected links, and *arcs* when referring to directed links.

To understand what is the difference between directed and undirected links, we first need to understand what means to have a link between two nodes. Being a mathematical representation of elements, a link represents the occurrence of a *relation* between two of them. The meaning

of such relations is ours to give, so for example suppose that we have two nodes called “Dante” and “Beatrice” and the relation we are interested in is “love”. Dante loves Beatrice, so we would say with a mathematical relation $\text{Love}(\text{Dante}, \text{Beatrice})$. Here, the position of the nodes is relevant: $\text{Love}(x, y)$ means: “x loves y”, while $\text{Love}(y, x)$ means: “y loves x”. In this example, Beatrice doesn’t love Dante, so, if we wanted to represent our relationships with a graph, we would have to use a *directed* graph, that is a graph which uses directed links and have an arc from Dante to Beatrice.

Suppose instead that we are interested in a relation such as friendship. We generally think that if an individual Foo is friend with Bar, then Bar is also friend with Foo, that is $\text{Friend}(\text{Foo}, \text{Bar}) \iff \text{Friend}(\text{Bar}, \text{Foo})$. This is called a *symmetric relation*. If we wanted to represent such relations with a graph, we would use an *undirected* graph, that is a graph which uses undirected links.

Edges (as well as arcs) can have weights attached to them, meaning that two nodes have a relation which can be quantified with a number. For example, suppose we are interested in representing the distance between nodes. Every node would have an edge with a number attached to it, which would represent their distance. In a mathematical representation it might be something like $\text{Distance}(x, y) = \text{Distance}(y, x) = k$, or in a logical representation $\text{Distance}(x, y, k) = \text{Distance}(y, x, k)$. A graph with weights attached to its edges is called *weighted* graph, if there are no weights it is called *unweighted* graph.

In this work we will use both weighted and unweighted graphs to represent our instances. To represent the interactions occurring between animals, we are going to use unweighted undirected

graphs, where an edge between two nodes would represent an interaction between them. By the definition of interaction we will use in this work, we know that it is a symmetrical relation, and we are not interested in the strength of such act, so it will be unweighted.

Sometimes, we will represent our input data with weighted graphs to show distances between nodes. Given the peculiar type of data we handle, it might not be the case that the graph is undirected. In that case, we would use directed weighted graphs to represent perceived distances between nodes.

3.2 Data Subdivision

To build a model able to accomplish the task we need it to do, it is usually necessary to have some data that it has to fit. This is referred as *training* data (set). To fit some data for a model means to extract some latent information from it in order to understand some patterns which lead to a specific prediction [28].

Once a model is learned, it is customary to test it to see whether it is effective at predicting some new data. We do not want to test our model on the same data we trained it with, because it might be the case that the model *overfit* the data, and would perform very badly with new, never seen instances of the input data. Overfitting occurs when the model is excessively complex with respect to the real function that describes our output [29]. Being so complex, what it really does is fitting a random noise in the training data, and how it behaves for unseen instances between two seen ones is most likely going to be random.

To overcome this problem, when we want to evaluate our model properly, we use a different partition of our data which has been untouched by our training process, that is called *test* data (set).

This partitioning of our available data is usually enough to train and evaluate simple models. However, sometimes this is not enough to give unbiased evaluations of our model.

Suppose we have an extra parameter that we want to fine-tune. We can imagine it being the order of our function, or the type of input given to the model, or completely different models. If we trained it with our training set and tested with our test set and then selected the parameter that maximizes our evaluation function, we would be overfitting with respect to the test set. Basically, we would choose the model that best fits our test data, but it would have unknown results for new, never seen data.

When we face this problem, we split our data into three partitions: the training, the *cross validation* (or simply validation) and the test sets.

Following the exact same reasoning done with just train and test sets, we will not touch our test set for all the tuning of our model, and we will instead train with our training set and evaluate with our validation set. In the end, after we choose the best model, we will see its performance against the test set.

We are going to use this partitioning policy to develop our model. Further details will be given once the needed background will be presented.

3.3 Markov Assumption

Suppose we are interested in knowing what the weather will be like today. We might suspect that the weather of today depends on the weather we observed the previous days. For example we might find out that if it has been sunny for several days in a row, it is most likely going to be sunny today as well, with a small probability of being cloudy, and it never happens to rain. If we wanted to model this behavior we would talk about conditional probabilities, for example, suppose that w_t is a variable representing the weather at day t, we would be interested in knowing $P(w_t|w_{t-1}, w_{t-2}, w_{t-3}, , w_0)$ which is generally different than $P(w_t)$. Although this would be a very precise estimation of the probability of a given weather condition for today, it is most likely impossible to have enough data to make it usable in practice, as well as being a very burdensome task. Suppose we find out that in reality, the probability of a given weather today is dependent on only a fixed amount of previous days, for example 2. Then, we would be able to compute its probability in a much easier way: $P(w_t|w_{t-1}, w_{t-2}, w_{t-3}, \dots, w_0) \approx P(w_t|w_{t-1}, w_{t-2})$. We call this a *Markov assumption* (in particular, a second-order Markov assumption).

More in general, we have a n^{th} -order Markov assumption if we believe that the probability of a given variable at time t depends only on the n previous times. Usually, this is not true, but it is a necessary assumption to make the problem tractable.

Now, suppose we know the relative positions of every animal we are observing with respect to any other animal at any time t. The best thing to do to find out if two animals are interacting would be to see all the previous history of the network. However, to do so, we would need an

enormous amount of data: suppose that we would need X instances to have a good estimation of a specific input configuration, then, every time we increase our Markov assumption by one, we would need to double the overall required input data for each input variable we consider at any give time. Also, this would be the lucky case where our variables had only two possible values, and we would have to triple, quadruple, etc. for a bigger range.

Thus, we need to make a reasonable Markov assumption. Suppose that the interaction between two animals would only be dependent on the actual time: then a zero-order Markov assumption would be fine. In general, we are interested in finding the best Markov assumption, that gives us good results w.r.t. the size of the data we have, without being too computationally expensive.

3.4 Cost Sensitive Learning

Generally, every classifier is built to maximize the accuracy of its predictions. Although it is usually what the user wants, sometimes this is not the case.

Suppose that we are predicting whether or not a patient has pancreas cancer. Surely we would like to accurately have only true positives and true negatives, however, when we are wrong, the two effects are dramatically different: if we have a false positive, we can just double check with maybe another method to be actually sure that he is ill. More in general, if he is in a hospital, he stays in the hospital and no harm is done. However, if we have a false negative, we would set the patient free and the next time he comes, his situation will be much worse than before.

In all the cases where a false negative is different than a false positive, cost sensitive learning should be done. Cost sensitive learning is also often used to diminish the harm of having unbalanced data, when sampling is not very practical or would worsen the results (such as when we don't have enough data).

3.4.1 Cost Matrix

If we want to represent the different costs of our classifications, it is customary to use a cost matrix, where the rows are the actual values and the columns are the inferred values. Sometimes in other papers the convention is the opposite, so we ask special care from the reader when looking at them.

TABLE I: OUR COST MATRIX: ROWS ARE ACTUAL LABELS, COLUMNS ARE INFERRED LABELS

	T	F
T	0	c_{fn}
F	c_{fp}	0

Usually both the true positive and true negative costs are 0, while very rarely true positives might have negative values to indicate profit. Given that the higher the cost the worse our model is at predicting, to evaluate a model while using cost sensitive learning, we will use a cost function which will simply multiply the number of predictions p_{ij} with the cost weight c_{ij} of that specific cost matrix and sum them all. Clearly, the lower the score, the better the

performance. To our purposes, we will have 0s on both true positives and true negatives, and have a higher weight for false negatives w.r.t. false positives. Table I shows our target cost matrix.

3.4.2 Classifier Adjustments

To make a classifier work with a cost matrix, adjustments must be made. We hereby discuss the most common methods used:

- Make the classifier provide probability estimates, compute the expected cost of each candidate and select the one which minimizes the cost.
- Sample the data during training phase in such a way to have uneven distributions of the classes, which will bias most classifiers to specific outcomes.
- Directly modify the inner workings of the classifier to make it use the cost matrix, which should maximize the fit of that classifier to that specific cost matrix.

The limitations of these approaches come from how specific classifiers work and the type of data we have available while training: most algorithms can't be modified to fit a cost matrix or cannot provide probability estimates. NNs can both provide probability estimates and modify their inner workings (the latter is preferred), but have a hard time sampling the input data when it returns multiple outputs. Given that what we usually want is to have a balanced distribution while training, a stronger weight in the cost matrix might be needed to impartially act as an equalizer.

3.5 Support Vector Machines

A Support Vector Machine (SVM) [30] is a model based on a supervised approach which can perform both classification and regression analysis.

It need as input a set of training data, each line labeled as one of the only two possible categories, and it outputs a deterministic binary linear classifier. It can also perform a non-linear classification by performing the so called ‘kernel trick’.

An SVM wants to find a hyperplane which can be used as a classifier between the two selected classes. Ideally, it tries to find a hyperplane that perfectly subdivides the two categories and selects among the many possible, the one furthest from all points. This is usually impossible to do, thus it uses a *soft-margin*, meaning that it tries to split its points at best, trying to minimize the cost of the misclassifications which are proportional to how far is the misclassified point from the right side of the hyperplane.

When a linear classifier is not enough, a transformation is used to represent our input data into a feature space that makes the dimension easier to be separated by a hyperplane. This operation however would be extremely time-consuming, thus a kernel trick is used: we don’t need to transform our dataset, we just need to perform a dot product of an N dimensional space with a $M > N$ dimensional space. This can be efficiently done with a kernel function, thus the so called kernel trick.

There exist several extensions for SVMs, which are not needed for our purposes, such as multiclass SVMs and support vector clustering.

3.6 Neural Networks

Artificial Neural Networks, or NNs, are a family of many models inspired by the real biological neural networks.

While they may vary a lot one another, they all have in common their basic structure, which consists of interconnected artificial neurons that send messages each other. An artificial neuron is usually modeled taking example from the Hebbian Rule in biology: basically we receive a number of inputs with some weights attached, we have a threshold called bias and we fire an output. From that, we can have many various implementations.

We are interested in supervised learning with NNs. While the details of these models are many, the general approach is, during training, to try to compute an output while giving a sample input, compute its error w.r.t. the expected output for every output neuron, and then use backpropagation, which is a method to adjust more the weights of the network which are most responsible for the error by using the gradient of its error.

In our work, we will use a fully connected feedforward neural network, which is the oldest and most commonly used, built however using mostly state of the art methods: Rectified Linear Unit (ReLU) activation function with dropout neurons and a Bernoulli negative log-likelihood error function.

A ReLU is a very trivial activation function: the idea is simply to have $f(x) = \max(0, x)$. This has been shown [31] to be more biologically plausible than the more common functions such as logistic sigmoid and hyperbolic tangent.

Usually, we prefer not to have 0 values, thus the rectifier function is smoothed: $f(x) = \ln(1 + e^x)$, which only gives positive numbers, still resembling the rectifier function.

Dropout is considered one of the most successful recent discoveries of the decade. During training phase, we randomly ‘drop out’ some neurons, setting their output to 0, thus basically not making them fire. During prediction phase, every neuron is allowed to fire. This has again a biological inspiration, from genes: when a child is born, it receives half its genes from both parents, thus every gene has to be able to adapt with unknown other genes, and be useful by itself.

This method has several advantages: it prevents co-adaptations thus avoiding overfitting and it results as a very powerful ensemble method, as it can be seen, while training, to train up to 2^n different networks, where n is the number of neurons, and while testing to merge them. This sometimes implies the need of a higher amount of data required or simply a longer training phase, but it has been shown to own the state of the art performance for several deep learning classification tasks.

3.7 Decision Trees

DTs are a very common type of classifiers. They use a tree to decide how to label an input instance, where the leaves are the class labels and the nodes are some conditions of the input that branches the decision to be taken.

DTs can either predict multiple classes or a continuous value, in the latter case they are called Regression Trees. This classifier is very popular, mostly because of its simplicity and its reasoning is understandable by humans and can be easily plotted.

A tree is built by greedily deciding what attribute to split at every step, selecting it by choosing a scoring measure. A very well known measure is the Information Gain, which tries to minimize the overall entropy of the system. Informally, we can say that $\text{Information Gain} = \text{Entropy}(\text{parent}) - \text{Weighted Sum of Entropy}(\text{Children})$. We do that for every possible child split and select the one with the maximum score. If a node already perfectly explains the data (it classifies all its data with just one label), it becomes a leaf. This process usually continues until or all nodes become leaves or there are no more features to split or the gain from splitting is less than a given threshold. Usually, branches get pruned also after this process, to reduce overfitting.

3.7.1 Ensemble Methods

DTs by themselves perform well, but they don't own the state of the art performances. Whenever we are not interested in having a decision tree representation and we only want the best classifier, ensemble methods come into play.

Ensemble methods consist of using more than one classifier to infer a label. How the result is chosen among the individual classifications may vary one method another. Ensemble methods work well when the basic classifier is simple and very susceptible to noise. Decision trees are the most common models used because of these needs.

The most common ensemble methods are:

- Bagging [32]
- Boosting [33]
- Random Forest [34]

The main idea is more or less the same for the three of them: we want to have a big number of independent classifiers, that means that ideally if classifier A says ‘Yes’, we don’t know anything about what classifier B is about to say. If every classifier has an accuracy greater than 50% and we take the majority vote, we end up increasing the accuracy ideally by as much as we want, depending on how many classifiers we use, because the more classifiers we use, the more likely it is that the majority of them classified correctly.

This directly applies to bagging and random forests, the difference is how they achieve the condition of independence of their classifiers (also, it is anyway impossible to have a perfect independence among them): bagging, or *bootstrap aggregating*, trains with up to the same number of data of the input data, however it samples them with replacement from it. This is shown to give $(1 - 1/e) \sim 63.2\%$ unique elements, while the rest are duplicates. Being decision trees very sensible to noise in the data, the resulting classifiers behave very differently. Of course, to have even less resemblance, a smaller number of samples can be taken.

Random forests do exactly as bagging, but they increase the classifiers independence by also ignoring a certain number of input features (usually they use the square root or half of such number), making them more prone to error, but still usually over 50%.

Usually random forests perform better than bagging, but, as we will see, this is *not* the case for our instances.

Boosting uses a slightly different approach: it keeps adding classifiers which specialize where the previous classifiers mispredicted the most. In the end, every classifier is weighted and besides predicting the label, it also gives a confidence on how certain it is. The final results are computed

by weighting the classifiers by also considering this confidence and the most likely overall result is selected.

3.8 Statistical Significance

Sometimes, we try different models to see which one performs best w.r.t. our data. Now, suppose we have two models which performed similarly, i.e. they had almost the same accuracy, precision and recall. Is really one better than the other, or are they coming from the same distribution, thus either one of the two is the same for us?

To answer these questions, we do a test of statistical significance: how likely is the null hypothesis to be true for the two output distributions of our models? The null hypothesis is supposing that the two populations come from two different distributions (there is no correlation between them).

A test of statistical significance computes a p-value, which is the probability of obtaining results at least as extreme given that the null hypothesis is true, thus they are from two different distributions. A significance level α is introduced to understand when this p-value is excessively small: α is the probability to reject the null hypothesis in the case it is actually true.

Thus, suppose that our p-value is greater than our selected α , then we would be confident with probability $1 - \alpha$ that the null hypothesis is true. However, if the p-value is less than our significance level, it is very unlikely for the null hypothesis to be true, so we reject it.

Different distributions use a different test, for example for Gaussian distributions, t-test is the most commonly used.

3.8.1 Multiple Comparisons

When we have to do multiple comparisons, the standard statistical significance tests become unfit for the task.

Suppose in fact that we are testing a new drug and we want to know if it is helping to cure any of 100 disease symptoms. To do that, we perform a test of statistical significance with a significance level of 5%, thus we have 5% chance to incorrectly reject the null hypothesis if it is true.

However, supposing that the null hypothesis is true for all 100 symptoms, that is, it doesn't have any effect at all, we should expect to incorrectly reject 5 of them. Moreover, the probability to have at least an incorrect rejection is as much as 99.4%.

To solve this issue, we want to adjust our significance level to be more stringent. One very common example is the Bonferroni adjustment, where from Boole's inequality we know that if we have k tests and a target significance of α , adjusting it to α/k for each one of them we are sure for the total error to not exceed α .

3.9 Sensitivity Analysis

Whenever we ask the questions: "Why does my model not work? What are the weak points of my model? Are there useless inputs? How robust to noise is my model?" we want to perform some sensitivity analysis. It is the study of how the uncertainty in the output of a model can be properly split among uncertainties in its inputs.

There are different ways to do these analyses. One widely used is One-Factor-At-a-Time (OFAT): as the name suggests, we modify one factor at a time while not varying the remaining factors to see what effects it produces to the output.

Sensitivity analysis is infamously known to be computationally expensive, thus a full analysis might be unfeasible, especially when we have a big number of factors we are interested in. Still, we are going to do as many experiments as we can, to thoroughly test our models.

CHAPTER 4

PROPOSED APPROACH

Our task is given a configuration and some data regarding such configuration, labeled at every interval with the interactions occurring among any animal, find the model that best infers those interactions. Ideally, to infer some interactions at time t , we can look at our input data at time $t - 1$, $t - 2$ and so on. So, for every timestamp t to infer, we can use several input data of time $t' \leq t$ to aid our inferences. Figure 2 shows an example of input and output data.

Moreover, we consider *false negatives* to be more relevant than *false positives*: There are three reasons for that:

- The expected interaction network is very sparse. This implies that the trivial model that claims there are no interactions will have reasonably high accuracy, but terrible recall. We want to avoid this scenario, of course, which means to be more biased towards having less false negatives than false positives.
- False positives can be removed manually after the inference, if they are not too many, while false negatives cannot.
- Having a high number of false negatives seriously worsens the quality of the inferred network, and its structure might look like random [26].

Of course, saying “every animal always interacts with everybody else” would give us a recall of 1, but a terrible precision. On the other hand, precision by itself is still not sufficient, because

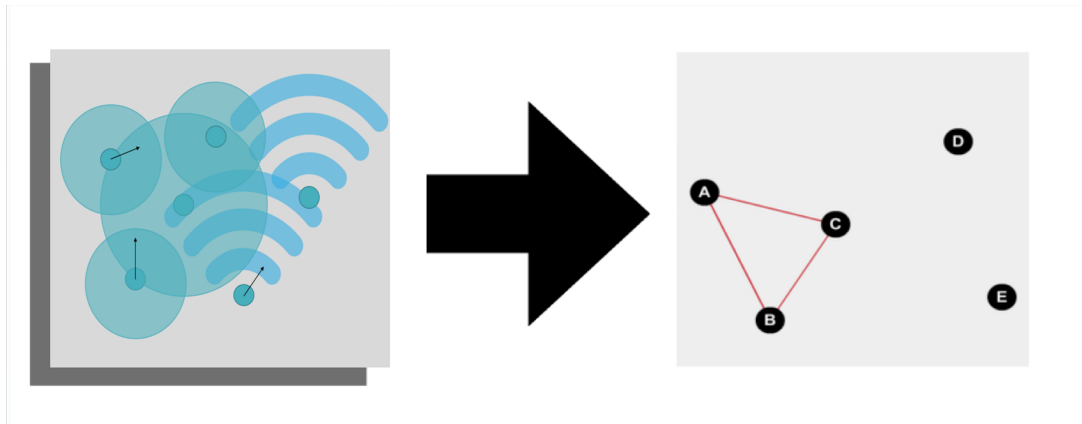


Figure 2: An example of inference: given several timestamps of sensor data, we want to infer an undirected graph of interactions.

we wouldn't be able to realize how many interactions we are missing. Thus, only using either recall or precision would not be enough to understand how good is our model.

This Chapter will further explain the proposed sensors we are interested in synthesizing, the models and the framework we built to respectively infer interaction networks in any configuration and understand when this model gives good results and when and why it doesn't. Section 4.1 will describe the sensors we want to synthesize. Section 4.2 explains the proposed model of this work. Section 4.3 will describe the proposed framework.

4.1 Proposed Sensors

We are interested in inferring the interactions occurring among animals, in order to build a graph of interactions for every given timestamp. If we want to infer interactions between two animals, knowing their absolute positions is not strictly necessary. What we would be

interested in would be their distances. Moreover, we would like to know the distances among all the animals we are observing, which might spot interesting patterns.

Having accurate absolute distances would be ideal, however the state-of-art technology doesn't allow us to have an accuracy as good to be used by itself for such purposes. GPS data, with an accuracy of 3 meters, is unfit to be used for most animals, especially the smaller ones. Adjustments can be done and it has been reported an average accuracy of 30 centimeters [21] on a controlled environment. However, its reliability is very dependent on the signal and obstruction of the line of sight with some satellites is likely to occur. Also, in certain cases such as with small animals, even if we always had the guarantee of 30 centimeters accuracy it would still be too much. What we could use to have more accurate information are pairs of BLE sensors (one transmitter and one receiver) [35] the receiver would sense a signal and attach to it an RSSI value [36], which stands for the strength of the perceived signal. If we tried to convert our RSSI value into absolute distances, it would result to a relatively high error but it would still be more informative than using pairs of GPS sensors.

Moreover, suppose we received two signals from two different transmitters, then we would have two RSSI values and we could compare them. This makes us have arguably more accurate relative ranking distances among sensors: we would be able to say who is closest to me, who is second, and so on. Of course, we would still use thresholds of uncertainty so we might end up considering multiple sensors as equally "second". Ranking distances might be of key importance to spot interactions, as studies show how animals interact with a fixed number of closest neighbors [3].

Also, for both the inaccurate absolute distances and the somewhat accurate relative ranking distances, it may well be the case that a receiver doesn't receive any signal from a specific transmitter. This might either imply that the transmitter is too far away to be spotted, or that the signal was obstructed and wasn't able to reach its destination. Thus, we are in the unfortunate situation where "missing data" might be caused by two completely opposite reasons. This will get our data even noisier than just the inherent errors of precision of the sensors. Still, having redundant sensors, or multiple sensors in different positions should spot these errors and overcome them.

Also, our animals can be equipped with Magnetic Pick-Up (MPU) sensors to either extract accelerometer and/or gyroscope data. We will disregard gyroscope data for our instances and instead sometimes use the absolute value of the speed extracted from the accelerometer. We also have the per-axis speed, however it doesn't really make a lot of sense if we are not planning to use absolute positions but only distances.

Now, let's look at the input data we are going to use: we said we want to transform our RSSI values in absolute and ranking distances. However, both transformations suffer from the absence of received signal. To be able to input something also on these cases, we need to have discrete domains for both absolute and relative distances.

Ranking distances as we defined them are already discrete: we would have the closest ones, the second closests one, and so on. The only thing we would have to add is a ranking representing when we don't spot any signal. We can either say that all those sensors are considered the furthest (i.e. if the furthest spotted is in third position, we would add a fourth

position for all the others), or we would define a default position for all of them (i.e. suppose that we at most are able to discern 5 ranking positions, we would add a sixth position that would refer to all the not received signals). To remain consistent with the concept of ranking, we decided to exploit the first option.

Absolute distances are continuous instead. However, we wouldn't be able to build a not-biased model with continuous distances and many not received signals. What we can do is to split the input in different ranges such as "very close", "close", "medium", "far" and a special distance "very far" for when we don't sense anything.

As mentioned before, when the input should be sufficiently near to be sensed but it doesn't for any reason, it worsens our input data. That is one of the reasons why we would like to add information such as fixed receivers around our grid, to overcome such problems.

Finally, notice how these discretizations give us an ordered domain, that is we are using *ordinal* values, so our model can exploit the knowledge that "medium" is further than "close" and "very close" but closer than "far" and "very far". Likewise for rankings.

Once we have these sensors available, we can decide on using several different configurations: first of all, for all possible configurations we can either have or not have accelerometer data from each animal. We might decide to put a transmitter on every animal and put some receivers on some fixed positions over them (for example onto some beacons). We would then receive ranking and absolute distances of every animal from every fixed position.

Or, we could attach both receivers and transmitters to each animal, thus being able to have distances directly among them. Notice that, being relative, we would represent it with a

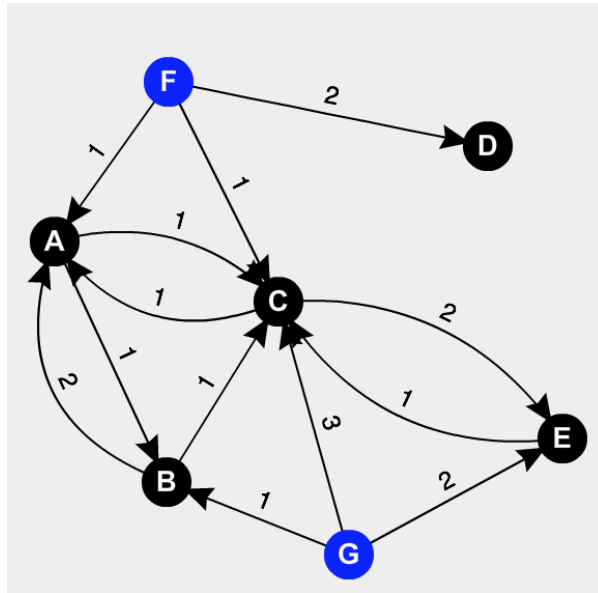


Figure 3: An example of input ranking distances data in a configuration with receivers on both animals and beacons. The black nodes are animals, while the blue nodes are fixed position beacons.

directed weighted graph, because it is not necessarily true that, given two individuals x and y , $\text{SensedDistance}(x,y) = \text{SensedDistance}(y,x)$.

Finally, we could have both configurations altogether: transmitters and receivers on every animal, and receivers in some fixed positions.

Figure 3 shows an example of input ranking distances data. As we can see, this is a directed weighted graph where distances are discrete positive numbers, there can be multiple arrows of the same rank starting from the same node, but there are no gaps in the rankings. Also, receivers only sense distances and are not sensed. We can see that sometimes receivers do not sense a transmitter, for example B senses C, but C doesn't sense B. Also, ranks between two

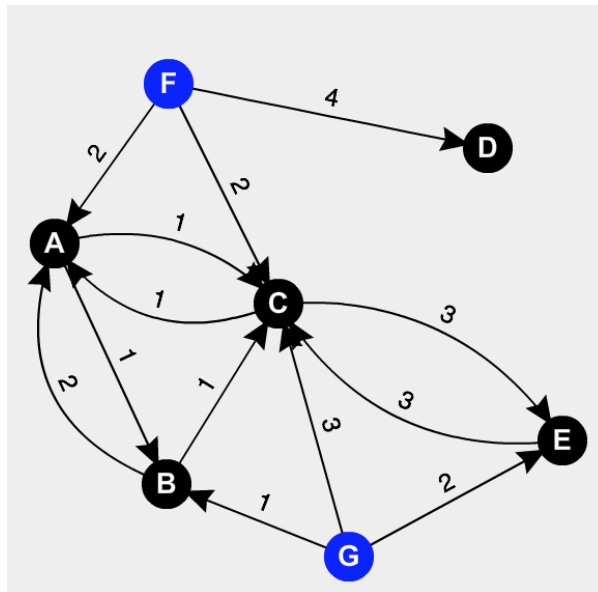


Figure 4: An example of input absolute discretized distance data in a configuration with receivers on both animals and beacons. The black nodes are animals, while the blue nodes are fixed position beacons.

nodes can be different either for noise in the data (pair AB) and for structural properties which have nothing to do with noise (pair CE, where E only senses C thus it is distant 1, but C senses A as well, which is closer, so it says E is distant 2).

Figure 4 shows a possible absolute distance input (already partially discretized) for the same timestamp. What wasn't sensed remains not sensed, however we can see that distances don't necessarily start from 1 (also, they could start from 0 if very close), there can be gaps and distances without noise are more consistent. In fact, even if pair AB due to noise gives a contradictory distance, pair CE this time spots the same distance from each other.

4.2 Proposed Models

Given some labeled data of a specific configuration of sensors, whose values are discrete ordinals and possibly floating point numbers (regarding speed in our examples, but not limited to them), we want to build a model which explains at best our data.

Our output will ultimately be an undirected unweighted graph of interactions. The first question we have to answer is: how do we want to infer the edges of our graph? We want to infer pairwise interactions one at a time, or more specifically, every possible dyadic interaction will have its own output, saying whether it is interacting or not at a specific timestamp.

We present two different families of models: an assumption free family, and one with independence and equality assumptions.

4.2.1 Assumption Free Family

Even if we want to individually predict every edge, this does not mean that we have to suppose that the presence of an edge is independent from all the other edges.

In fact, if we feed our model with all the input data we have at any given time, and we individually predict every edge from such data, this makes every edge possibly dependent from the others, even if we were to predict such edges one at a time (notice that it is *not* always the case).

To understand why they are dependent, imagine what we would do if we considered every edge to be independent to the other edges. For now, consider a simple configuration, which can be easily generalized to all our cases, where every animal has both a transmitter and a receiver and we want to classify an edge between two of them. If we believed in edge independence,

we wouldn't care about any data regarding any pair of animals but the ones we are classifying now (why caring about the distances between animals 3 and 4, if we are analyzing 1 and 2? Also, why caring about the interaction between 2 and 3, when interested in 1 and 2, if the presence or not of an edge between 2 and 3 does not imply anything for 1 and 2?). Interestingly enough, the concept of "ranking distances" starts being less useful (why caring to know that 2 is second in distance to 1, if we don't care about other interactions?), however it should still be useful by itself, considering that animals are supposed to interact with a fixed number of closest neighbors, as previously noticed [3]. Likewise for speed, we would only care about their two values.

Generalizing, if we had fixed position receivers, we would be interested in only the signals received from the 2 animals we are considering.

Knowing that edges can be dependent from other edges makes all our data useful for their classifications.

Also, we consider every animal to be possibly different in behavior w.r.t. every other one, so we want our models to exploit this fact by specializing in a different way for every possible dyadic interaction (this will usually result in having multiple specialized classifiers). Notice that they would still have all the available input features, but the number of outputs of our overall model is equal to the number of possible interactions at every timestamp.

This family of models is able to specialize and spot group patterns, thus it is expected to perform best with a lot of data, but fairly poorly with a small amount.

4.2.2 Independence and Equality Assumption Family

On the other hand, if we assume the likelihood of an interaction to be independent from all other interactions, and if we suppose that every animal behaves the same, or in a more technical way, we are interested in the general concept of interaction regardless of what pair of individuals we are interested in, we can drastically drop both the input feature size and the size of data required to have a good classifier.

In fact, we could create one single classifier which would infer every interaction at each timestamp, by modifying its inputs every time: as we noticed before, in this case we would only be interested in the input features regarding the pair, that are pairwise distances, speed, and beacons distances sensed for the two individuals. If we feed this information to our model, regardless of what pair we are interested, it will give us an output.

As you can imagine, this drastically decreases the size of data required: for n individuals, from n^2 outputs (which usually means classifiers), we now only have 1 output. This can usually be trained with a very small amount of data and still give reasonably good results.

Of course, this has its shortcomings as well: aside from being it trickier to be handled, because it would need a more complex preprocessing of data, and in general an input format following some rules (we use dictionaries of dictionaries in our Python implementation, while the assumption free model accepts matrices), making it less user friendly, it clearly is unable to spot collective behaviors and it would not be able to specialize for each individual.

It might be questionable why we consider *good* to specialize for individuals. This might be wrongly identified as overfitting, but most of the times, to perfectly spot an interaction with no

false positives/negatives is usually impossible because the amount of sensors needed and where to put them on the animal is unreasonable or practically not doable. For example accelerometer data for arms movements on baboons is extremely tricky because baboons would most likely destroy the devices. Therefore, knowing that a specific animal is more likely to interact w.r.t. other individuals, with lack of important data, is extremely precious.

This leads us to suppose that this family of models would perform extremely well with a little data, and worse than the more general family with medium to a lot of data.

4.2.3 Proposed Classifiers

In practice, we consider a baseline approach and several different models that can be used with any of the two families:

- Baseline: distance and time threshold
- NNs
- SVMs
- Ensemble methods for DTs

4.2.3.1 Baseline Classification

Our baseline approach assumes that both transmitters and receivers are on each animal and disregards the preprocessing of the data into ordinal categories: It wants to find, for each pair of animals, the maximum distance and for how long that distance must be kept to consider it an interaction.

We only consider the distances between the two animals we care about, thus we can have at most two input values for each pair, and if at least one of them is sensed to be closer than the threshold, we consider them close. If they remain close for the minimum time threshold, we consider it an interaction. If no signal has been sensed, we consider it to be ‘far away’ and no interaction is spotted.

We want to find the couple of thresholds that minimizes our cost function. The maximum distance threshold is clearly the maximum range of the receivers, while the time threshold is a parameter to be chosen. However, the optimal threshold is hardly ever going to be greater than 3, thus we could select 3 for most instances, and only if 3 happened to be the optimal threshold for a specific instance, we might want to increase this number.

This baseline is simple enough to be able to find the best parameters (global optimum) by a bruteforce approach. Heuristics that find local optima in logarithmic time with respect to the range of the receivers exist, but are not needed in this case.

4.2.3.2 Neural Network Classification

Neural networks seem ideal for our target configurations: they can be built to have any number of numeric inputs as well as any number of binary outputs. Moreover, even if just slightly, mispredictions of one output modify most of the network which is shared by all outputs, thus actually being theoretically dependent from the other outcomes. We used a fully connected feedforward neural network with dropout ReLU neurons for all but the output neurons, and for output neurons we used a standard sigmoid activation function where being close to 1 means interaction and being close to 0 means no interaction.

One problem with NNs is that their input data cannot be balanced (for the assumption free family). We can theoretically decrease the unbalance of 0s w.r.t. 1s by completely discarding train data without a single positive classification, but this, especially for networks with a lot of nodes, doesn't solve the problem.

Here, we decided to not discard training data (because it was not needed for our tested instances) and to balance the problem by using cost sensitive learning: we took the Bernoulli Negative Log-likelihood error function described this way where x is the inferred and y is the expected value:

$$\text{error}(x, y) = -y \ln x - (1 - y) \ln(1 - x) \quad (4.1)$$

noticing that

$$\text{error}(x, y) = \begin{cases} -\ln(1 - x), & \text{if } y = 0, \\ -\ln x, & \text{if } y = 1. \end{cases} \quad (4.2)$$

thus, suppose we have a cost matrix where mispredicting false negatives and false positives have a cost of fn and fp , respectively, where in our case $fn \geq fp$, we want to weight this error function to backpropagate differently those two types of error. First of all, we normalize the two weights so that we are sure to find convergence: $w_{fn} = fn / \max(fn, fp)$ and $w_{fp} = fp / \max(fn, fp)$ so that the weight for the bigger cost will remain 1 and the weight for the smaller one will be reduced proportionally. Then, we multiply the two parts of our former cost function accordingly:

$$new_error(x, y) = -w_{fn}y \ln x - w_{fp}(1 - y) \ln(1 - x) = \begin{cases} -w_{fp} \ln(1 - x), & \text{if } y = 0, \\ -w_{fn} \ln x, & \text{if } y = 1. \end{cases} \quad (4.3)$$

What it means is that if we mispredicted and $y = 1$, then we must have said that $x = 0$ thus we had a false negative and we backpropagate multiplying its error with a w_{fn} factor, likewise for false positive errors, accordingly to our goals. In fact, even if the data is inherently unbalanced, by weighting less the false positives, we effectively help our model in being more balanced.

4.2.3.3 Balancing Data

The remaining classifiers have the way we handled data in common:

We created one classifier for every possible output, effectively creating $n(n - 1)/2$ binary classifiers which specialize in a single edge for the assumption free family (and of course, only 1 for the other family). This number, although being linear w.r.t. the size of the output, is easily handled for small to medium size networks of animals, which is always going to be the case for these kinds of inferences.

This trick makes our input data easily balanceable: we can always use all the minority class input instances and the same number, randomly sampled, of majority class input instances. Experimenting this turned out to make us *not need* to use cost sensitive learning, even if it was possible for all of the following models.

While there is nothing more to add for our SVM models, we still have to discuss our ensemble methods.

4.2.3.4 Ensemble Methods for Decision Trees

We tried three different ensemble methods with DTs:

- Bagging with a sampling size of 50% of the data and 100 trees.
- Random Forest with 100 trees.
- AdaBoost boosting with a maximum number of 100 trees.

AdaBoost is one of the most used boosting ensembles on the market. While we can't ever suppose a priori which will perform best between AdaBoost and the two more similar Bagging and Random Forest, we don't even know which of the latter two will perform better than the other.

In fact, the main idea of Random Forest is to increase the diversity of the classifiers by selecting only a small number of input features. However, we already know that there are going to be a very, very small number of features which are going to be extremely important for classifications, while the others will impact our results much less. Thus, randomly removing a big number of features implies to very usually not have *any* of the most important features.

We expect this to often result in a worsening of the results, because it will decrease drastically the average accuracy of every classifier, even if increasing the diversity. Still, we don't expect Random Forests to perform badly: the only condition they have to meet to give good results is to have an accuracy higher than 50%, and with a binary classification this is extremely easy to

achieve, even with not so important features. Thus, it will be interesting to see what impacts best the results: will it be a higher accuracy or a higher diversity?

4.2.3.5 Markov Assumption and Data Subdivision

Up to now, we only considered the input data of the specific time we want to label. This is a zero-order Markov assumption and it is not necessarily the case that it holds.

It could be the case that the distances of our animals of one, two, etc. previous time periods might well alter the likelihood of an interaction. Thus, we would like to try different assumptions. To do that, we need several things:

- A way to compare two results.
- To split the data into train, validation and test sets.
- Understand when to stop increasing our order of Markov assumption.

In order to understand if a bigger order model would eventually overfit the data, we need to evaluate our results and compare them: if we find out that a bigger order Markov assumption behaves worse than a smaller order, we would select the lower order one.

This implies that we need to test our models while training, thus we need to have a validation set to not overfit the test set. The test set will only be used at the end of every model tuning.

To evaluate our performances we will use a cost function directly extracted from our cost matrix: the lower the result is, the better our model is.

Finally, it might be the case that using a higher order assumption only slightly increases our results. This is a good hint for understanding that the proper assumption was the previous

one, because it means that adding new information doesn't improve our model. But what if a higher order actually improved the results? Using a threshold of improvement is not the best way to tackle the problem. What we will do is make a test of statistical significance between those two models, using the multiple comparisons approach. If the two models are most likely going to not be statistically different, we would refuse the higher order assumption to select the lower one.

Speaking of the statistical test, we will always refer to a Bonferroni multiple comparison test with $\alpha = 5\%$. Also, we performed a slight adjustment to it to better fit our goals: we are interested in having the simplest model which performs best. Suppose we had 100 outputs and we validated our model with Markov orders 0 and 1. Imagine our second order model to give a just slightly better evaluation result. We would then perform a statistical test and through Bonferroni adjustment we might find out that out of the 100 outputs, only 2 are statistically different. This might indeed mean that those two outputs are the main reason why it performed better than the smaller order model, or that again by chance they performed better just in this case. In fact, the more outputs we have, the lesser it is important for one single output to be better than the others, and increasing the Markov order implies significant computational costs. Thus, we decided to use the same $\alpha = 5\%$ threshold once again: in order to consider a model sufficiently better than the previous one, once Bonferroni adjusted, at least α outputs must be significantly different than the previous ones. To give an insight to why this looks like more ideal, if we had up to 20 outputs, this threshold would do nothing, and one different output would be enough to be a significant difference. However, for 100 outputs, 1 different output

may very well be by chance, and even if it weren't it would justify a whole Markov order more. On the other hand, if 5 of such outputs were to differ, we have reasons to believe that our new order is really helping and it is worth to be taken.

4.3 Proposed Framework

In order to evaluate our proposed models and to perform sensitivity analyses on them, we first need to be able to synthesize our data. Also, we need to do it in such a way that it is easily possible to fine-tune its parameters that impact the reliability of the input data.

4.3.1 Creating the Environment

Accurately synthesizing some real data is a very complex task whose results are very often far from perfect.

The background setup is straightforward: we create a virtual world, where we put inside a given number of animals with some transmitters and possibly receivers and eventually also put pillars in fixed positions with some receivers. We make our animals 'move' a fixed number of times while sampling either the values from our sensors and the occurring interactions every k steps with k not necessarily being equal to 1.

During this process we stumbled across three major design issues:

- Simulate the data retrieved from our sensors.
- Simulate the behavior of our animals
- Label the interactions of our animals

4.3.1.1 Simulating the Data

How do we design our sensors? Which parameters do they take? How are their outputs presented to us?

We want our sensors to give us data similar to RSSI values. Their absolute values are not relevant as long as their relative values are consistent, but we expect our sensors to fail sometimes and even when they don't fail we expect to have some noise in the values received.

We know that our receivers are unable to spot signals further than a given range, thus we could easily say that if the two sensors (one transmitter and one receiver) are distant more than that range, the receiver doesn't receive any signal. But what about when they are not as far away?

If we want to model the possibility of failure, we can just assume that every transmitter has a probability of failure to transmit a given signal and likewise for receivers if needed.

The strength of the signal sent can vary for several reasons, and that can be modeled by using a Gaussian noise which modifies the position we infer (instead of using RSSI values we directly estimate the distances between the two sensors, which requires one less computational step and gives us the same results).

However, when we do receive a signal, it is unlikely to be noiseless. We want to add some noise to it, also, the further it travels, the bigger the noise we can receive. We model this by using a Gaussian noise with mean 0 and a parameter for the standard deviation which decreases linearly the closer the two sensors are.

The good thing about it is that those parameters can be fine-tuned for our sensitivity analysis and fairly accurately describe the real world examples.

4.3.1.2 Simulating Animals Behavior and Labeling

The last two issues will be solved together, but before explaining how, it is important to understand why such things are difficult to deal with.

If we want to synthesize data properly, we want to have inputs reasonably close to reality, thus simulating animals behavior becomes crucial for our framework. Clearly, if animals didn't move at all, or moved at random all the time, their behavior would be useless for our purposes. Our goal is to be able to construct a animal which resembles sufficiently the behavior of a real animal, but not so much in details to have too many arbitrary parameters which could make us jump into false conclusions. For example, the field of view of animals different from fish is in most cases unknown. Now, if we had to rely to this information while synthesizing data and we weren't certain about its value, our results might drastically differ from reality. While, if we had a more general case where we knew that somehow something close enough is seen, this weaker assumption should hold for the real cases also.

For labeling we have yet again a problem: we can't manually annotate interactions after creating some data. Well, in theory we could: we would first create our input data, then we would have to plot it somehow and to manually say at every timestamp which are the interacting pairs. After all this is what we will have to do with the real data, so what is the problem?

Fist of all, one of the main goals of our study is to estimate *how much* data we need to label in order to build a reasonable model to spot interactions, so we don't know this information

here yet. Connected to this rises the second problem: we want to synthesize a variable amount of data, from a lot to very little, an enormous amount of time to perform sensitivity analysis. Ideally, this type of analysis can be made automatically, thus we really can't manually label our data, and even if we could, it would probably require years.

So how do we automatically label our data? We could say: if two animals are closer than a certain threshold for a certain time threshold, then they are interacting. The problem with that is *it is too simple*. We want to have challenging interactions to be spotted, otherwise we could wrongly believe our models are good, while they are good only for trivial cases.

As anticipated, we solved these two problems at the same time: we performed a very simple instance of agent based modeling [37], by building a Finite-State Machine (FSM) artificial agent intelligence. Agent based modeling is a very wide and complex field, and this work does not intend on going in depth into that. Given that our needs are not having extremely accurate behaviors (which for most animals would be impossible to have, otherwise we wouldn't need to observe them in the first place), a simple FSM with random transitions will suffice.

We decided to model the behavior of every animal as a machine which lives in several different states, and that behaves differently accordingly to its actual one. It must have a movement function which can switch states as well as performing its state behavior.

This FSM must of course be handled case by case, and the only requirement it has, is to have a special *interacting* state: in this state, an agent is interacting with at least another one, and we know who it is interacting with. This makes our labeling of interactions trivial: at any timestamp, we just look at every agent, if it is interacting, we add an edge of interaction with

every one it is interacting with. Even if our interacting behavior is somehow directed for now, we can still create an undirected edge (or directed if preferred).

The nice thing about that is we never miss an interaction, being as close as possible to a perfect labeling. If we don't believe it to be the case, we can add uncertainty to the automatic labeling. However, sensitivity analysis about that is far from useful, because it would be useless to say to our labelers: 'Be sure to be accurate at least 87% of the time!' because we are supposing that they are as accurate as they can be and they wouldn't know to be mistaken most of the time.

Finally, this gives us the possibility to actually label a specific behavior not by using our input data, thus our models will need to reverse engineer the correlations between our input data and the labelling, which is, said in a less fashioned way, performing supervised learning.

CHAPTER 5

CASE STUDY

We propose a case study where we synthesize some data and do some sensitivity analysis on it, to show example of how our framework and model work and evaluate our methodology while possibly giving some insights on general properties of dyadic interactions.

As anticipated, we need to create a random agent FSM: we decided to make one very simple agent which lives in four different states, and that behaves differently accordingly to its actual one. We made it fairly simplistic to avoid making assumptions of any type. It has a body and moves not much more than its body length for every timestamp, but we didn't assume how it senses any other agent, thus it has no explicit sensory system. Every number you will see is a specific instance of our more general parametric model. Of course, their numbers will be pure (without a dimension such as distance in meters or time etc.), but for the readers' clarity we will interpret them as centimeters.

The four states actually implemented are the following:

- Normal
- Hungry
- Sleeping
- Interacting

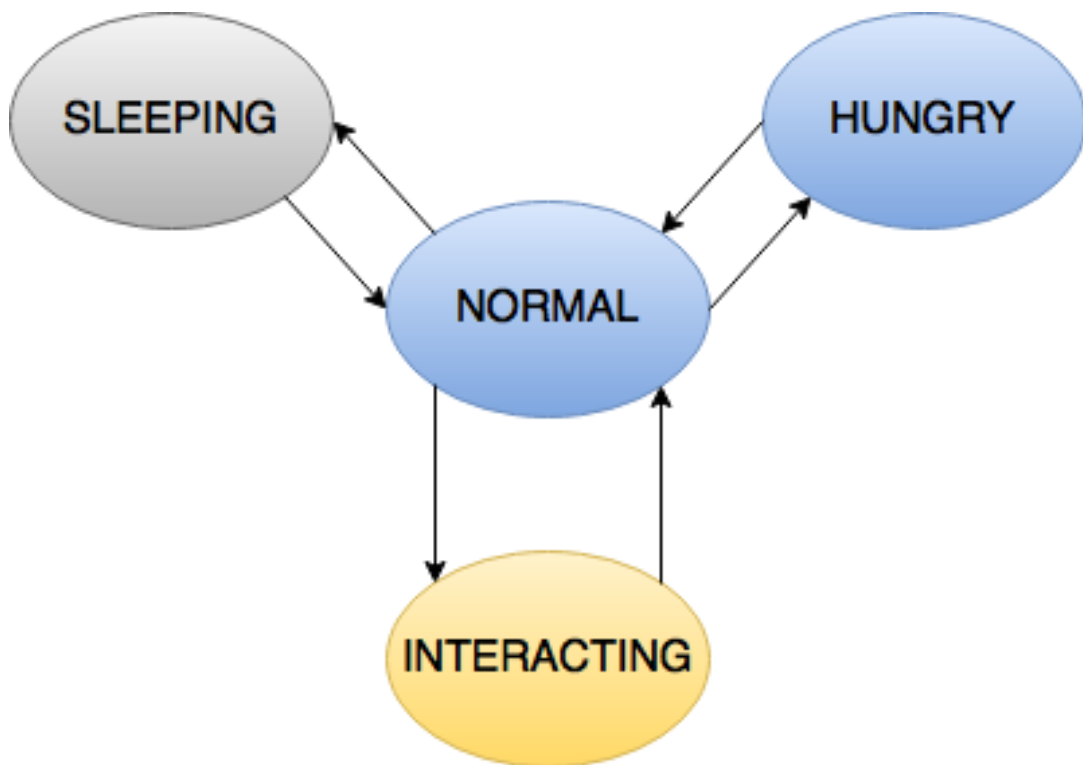


Figure 5: The actually implemented FSM of our agents. Transitions from states are random, although their chance may vary.

Figure 5 shows the FSM of our agents. The Normal state is the core of our automaton: it can either behave ‘normally’ or it can switch to any of the other three states. If it behaves normally, it can either stay still or move, where to is irrelevant.

Randomly, the agent can switch from Normal to Hungry state. When it does, its priority becomes to feed. To implement this behavior we created in our virtual world a spot where our agents can eat food (and ideally drink), when an agent is hungry, it doesn’t anymore behave at

random, but it instead moves towards the food spot of the fence and eats there to its heart's content (conveniently modeled by a number). After that, it goes back to Normal.

Or, starting from Normal state, the agent can decide to go to sleep. If it goes to sleep it doesn't move at all for a variable number of turns. After that, it wakes up and goes back to Normal.

Finally, it can try to start an interaction: if the agent is in Normal state and wants to interact with another agent, it can look around itself: if there is another agent close to its position, it can start interacting with them. This has a completely different behavior than the general case: the interacting agent starts moving towards and around the other agent (simulating either a poke or some active jumps around the other individual). Moreover, being playful increases the chance to interact with any other close agent. If it is interacting with more than one agent at the same time, it randomly decides who to torment. Also, it randomly decides whether to drop an interaction with an agent at any time and, if there are no more interactions active, it goes back to Normal.

In details, we implemented our agent behavior with these parameters:

- Normal state is the starting state of any agent.
- While in Normal state, it can transition to Hungry or Sleeping states with 5% chance each, and if sufficiently close (there is at least one other agent closer than 50 cm to our target agent) it has a 20% chance to transition to Interacting state.
- An agent in Sleeping state stays there for a random number of timestamps varying from 3 to 20.

- An agent in Hungry state, once reached a feeding spot, stays there for a random number of timestamps varying from 1 to 4.
- While in Interacting state, an agent can start interacting also with another agent very close to it (less than 30 cm) with a 30% chance. However, any occurring interaction can drop with a 40% chance at the beginning of every timestamp.

The interacting likelihood is a parameter we will modify later, to make interactions occur less and less often to make sensitivity analysis on our models.

Modeling an animal this way is reasonably similar to a real animal behavior (which still needs several parameters to be set to better resemble them, such as sleeping time, movement chance and so on), but not as specific to be close to one specific type of animal, and does not assume anything like the line of sight, hearing and smell of an animal, which is usually unknown.

Notice that this behavior construction is made purposely to have hard time inferring interactions from our model, and being it as general as possible, it should apply and give a lower bound for our parameters in real configurations, or at least an idea to what to expect.

However, this is only an example and it can be either made simpler or more realistic: Some examples for improvement are: to really model the starving factor of an animal as well as its fatigue which directly affect which state is most likely to be selected. To model the orientation of an animal and its field of vision (otherwise the orientation would be useless). To say that if you are sleeping and an interacting animal pokes you, or even every time a animal stumbles across you, you have a chance to wake up. Or, if some animal is interacting with you and you

are not sleeping or hungry, you have a very high chance to either avoid it, or start interacting as well. If you are willing to have a more realistic interaction, it is implementable in our framework in theory. However, once the complexity of the agents becomes reasonably big, we suggest using specific tools for agent based modeling such as NetLogo [38]. Nevertheless, care is recommended if following that route: setting the wrong (very specific) parameters w.r.t. the real animal's might result in misleading results.

We will put our agents in a $M \times N$ (5×5 is what we arbitrarily decided) m^2 fence. Whenever we say we use fixed position beacons in this work, we will refer to a configuration where beacons are positioned in a very redundant way: they are positioned in a grid, where their distance from either a wall or another beacon is exactly as big as its range, thus we are confident that an agent would be sensed by at least two beacons in most places, if there weren't reliability issues. Figure 6 shows our target positions of beacons.

First, we have to estimate some parameter thresholds regarding error and reliability of our sensors. We don't suppose our sensors (both transmitter and receivers) will be 100% reliable. Thus, we will estimate that their reliability, that is the probability to send/receive a signal, will never exceed 95%. Also, in our synthesized world we could be 100% sure of the distances between the two sensors, thus we add positional errors being sent from the transmitters and a distance error being received by the receiver. They are both coming from a Gaussian noise, where we give as input parameter the standard deviation.

A reasonably starting value for these errors is, given that the maximum sensed distance is 100 cm, we give a transmitter standard deviation of 10, and receiver distance standard deviation

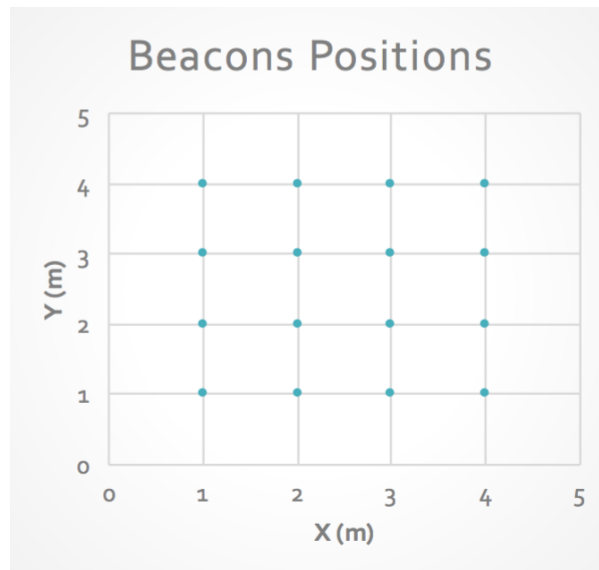


Figure 6: Positions of beacons in the synthesized world. The blue dots represent the beacons containing the receivers.

of 15. Thus we suppose our signals to be reasonably noisy to begin with because it wouldn't make much sense to suppose no noise in our default case.

For all our evaluations, we will always use a test size of 2000 time frames. This is big enough to give us relevant estimates of our results, but more importantly it is necessary to always have the same arbitrary size once decided, to be able to compare results with different parameters. Also, we will use a cost matrix where false positives are weighted 1, false negatives are weighted 3, and true positives and negatives have 0 weight whenever we don't specify otherwise. Notice that, while a cost function is needed for our models to properly finely tune our classifiers, its result once trained is negligible and we only care about recall and precision.

Anyhow, input size is the most important parameter to estimate as first: the lower the input size needed, the faster all our other analyses will be.

Also, as the generation of the data is a random process, as well as some inner calculations of our classifiers while being trained (think of how a Neural Network gets trained, or a Random Forest, for example), we want to repeat every analysis multiple times and average results. We decided 5 to be the number of repetitions, only for computational constraints (some of our analyses are too long to be repeated more than 5 times for every classifier). Thus, whenever we show evaluation measures, they are all averaged from 5 runs. Given the variability of our training phase, we believe that a greater number of tests for each model would be more insightful. However, as you will see shortly, the variance of our models does not seem like to be a primal concern.

Finally, special care must be taken with the parameters regarding our agents: they are very complex to be finely tuned. At first, we are supposing to have 6 (a partially arbitrary starting number, driven by the fact that a small number of agents should suffice in showing patterns and that real world labeling would start with a small number of animals first, however why exactly 6 was a preference of the author) agents which interact relatively often when they are close (20 % as stated before) in a time frame. This can and will later be significantly reduced to see how our models behave with much more unbalanced data. Also, this work will always put one receiver and transmitter on every single agent, although future analyses might be done to see what happens with different configurations.

We will start our analysis with the assumption free family of models, to understand how it performs, to give insight on several parameters, and we will introduce our other family later on, to compare the two of them in different contexts.

To give an insight of what data without noise would give as a result, we performed two tests, one without (Table II) and one with beacons (Table III), where there is no noise whatsoever. We will also show its uncertainty, so we performed 10 runs each (twice what we will do after this) to be more precise on the analysis.

TABLE II: EVALUATIONS OF SEVERAL MODELS FOR A CONFIGURATION WITH NO BEACONS AND A TRAINING SET OF 10000 SAMPLES WITHOUT NOISE

Method	Cost	Accuracy	Precision	Recall
Baseline	12371 ± 643	0.677 ± 0.019	0.390 ± 0.014	0.800 ± 0.018
SVM	13857 ± 630	0.638 ± 0.022	0.356 ± 0.017	0.776 ± 0.016
NN	8793 ± 1184	0.782 ± 0.018	0.506 ± 0.008	0.834 ± 0.049
Bagging	7753 ± 1091	0.784 ± 0.028	0.509 ± 0.021	0.906 ± 0.016
Boosting	8169 ± 966	0.774 ± 0.025	0.496 ± 0.02	0.896 ± 0.015
Random Forest	8136 ± 868	0.775 ± 0.021	0.497 ± 0.018	0.896 ± 0.019

We can see from Table II and Table III that bagging performs better than any other classifier with no beacons, and random forest performs better with beacons. This might be because when we significantly increase the number of input features, having a higher variability in our default decision trees is better than having a higher accuracy. However, we can also notice that our

TABLE III: EVALUATIONS OF SEVERAL MODELS FOR A CONFIGURATION WITH BEACONS AND A TRAINING SET OF 10000 SAMPLES WITHOUT NOISE

Method	Cost	Accuracy	Precision	Recall
Baseline	12085 \pm 610	0.687 \pm 0.013	0.397 \pm 0.009	0.796 \pm 0.016
SVM	10759 \pm 474	0.710 \pm 0.014	0.422 \pm 0.008	0.846 \pm 0.010
NN	19720 \pm 1509	0.731 \pm 0.053	0.196 \pm 0.144	0.121 \pm 0.094
Bagging	7863 \pm 859	0.782 \pm 0.021	0.504 \pm 0.018	0.900 \pm 0.022
Boosting	8147 \pm 704	0.776 \pm 0.017	0.496 \pm 0.017	0.892 \pm 0.021
Random Forest	7763 \pm 729	0.784 \pm 0.019	0.506 \pm 0.021	0.904 \pm 0.017

top performing classifiers don't gain much from having beacons when there is no noise, hinting that fixed positions don't help for spotting interactions. We can also notice that NN performs terribly with beacons, which we will discuss later, and that SVM improves significantly in both precision and recall. Finally, notice that the variance of our models is not of crucial concern, especially for recall.

5.0.1 Graphs and statistical tests

One very important issue to address before starting is how we are going to analyze and compare our results. One thing we can surely do is plot some graphs, for example the values of a certain evaluation measure with varying parameters of multiple models. This will give us a very intuitive insight for comparing different models and varying parameters. As we are performing multiple runs for each assignment of parameters, the canonical way to plot such information would be by using box plots, which would show median and variance of every model for each assignment. However, we realized that graphs this way were either too big

(if we were to show one assignment at a time) or too messy (if we wanted to plot everything altogether). Thus, we decided to only show the average of the runs for each parameter while plotting graphs. Also, when the x axis is a parameter, we will connect points of the same model with a line. Given that if we had boxplots we wouldn't connect them, this is a controversial choice. However, as we want to show trends occurring while varying parameters, and that if we didn't use lines some points would not be visible because of them being too close to others, we decided to adopt it regardless.

Anyhow, we are not going to disregard the fact that these are distributions and not fixed points. In fact, we can directly compare two classifiers by looking at their averages and variances for some evaluation functions, such as recall or precision. We will first perform normality tests (Saphiro-Wilk [39]) for the outcomes of our classifiers and once confirmed they seem normally distributed, we will perform unpaired t-tests to see if two classifiers are significantly different, or one-way ANOVA if we are interested in confronting more than 2 classifiers altogether.

As a first test, we tested normality for all our classifiers with no noise with respect to precision and recall and they didn't result *not* normal.

5.1 Estimating the Training Size

Estimating the size of the training data needed to have reasonable results is extremely important. We will have to estimate them for at least two configurations:

- Without fixed position beacons holding receivers.
- With them.

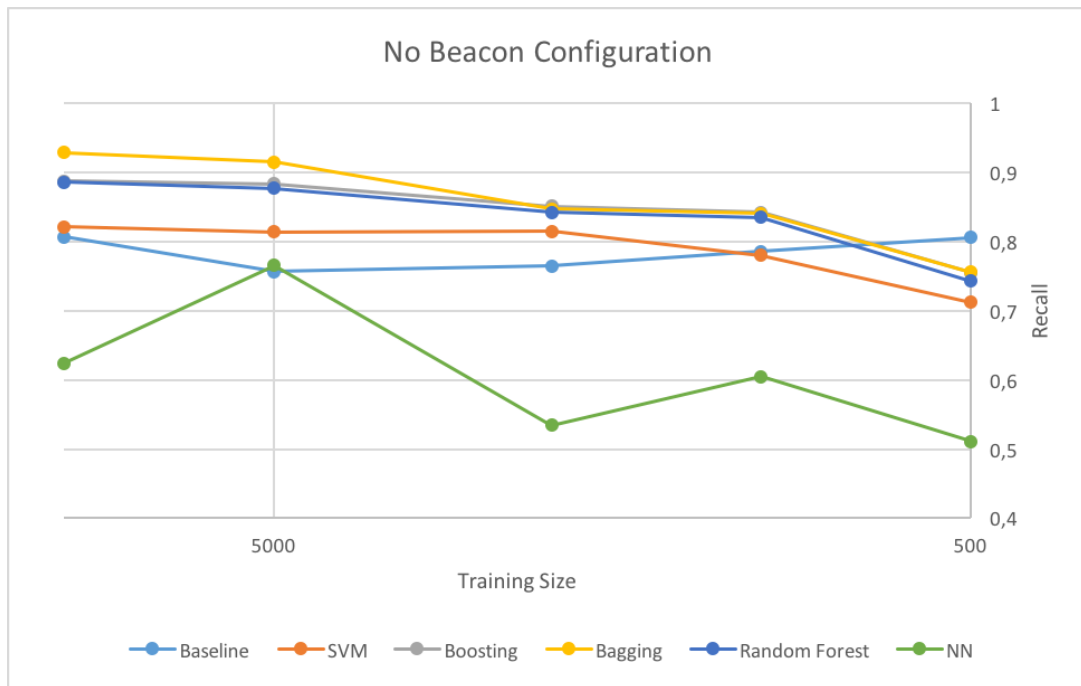


Figure 7: Recall evaluation of our selected models with different training size and with no beacons.

The reason is simple: the size of the input features significantly increases when we add those beacons, thus it may be the case that a small size of data for the first configuration is not enough for the second.

We will start without beacons and see how our models behave with gradually less data: We start from 10000 time frames which we believe it to be reasonably high (it would mean that 10000 different time frames would have been manually labeled, which is unlikely), and go downwards in a non linear fashion. We will stop once we realize our family of models is deteriorating too much:

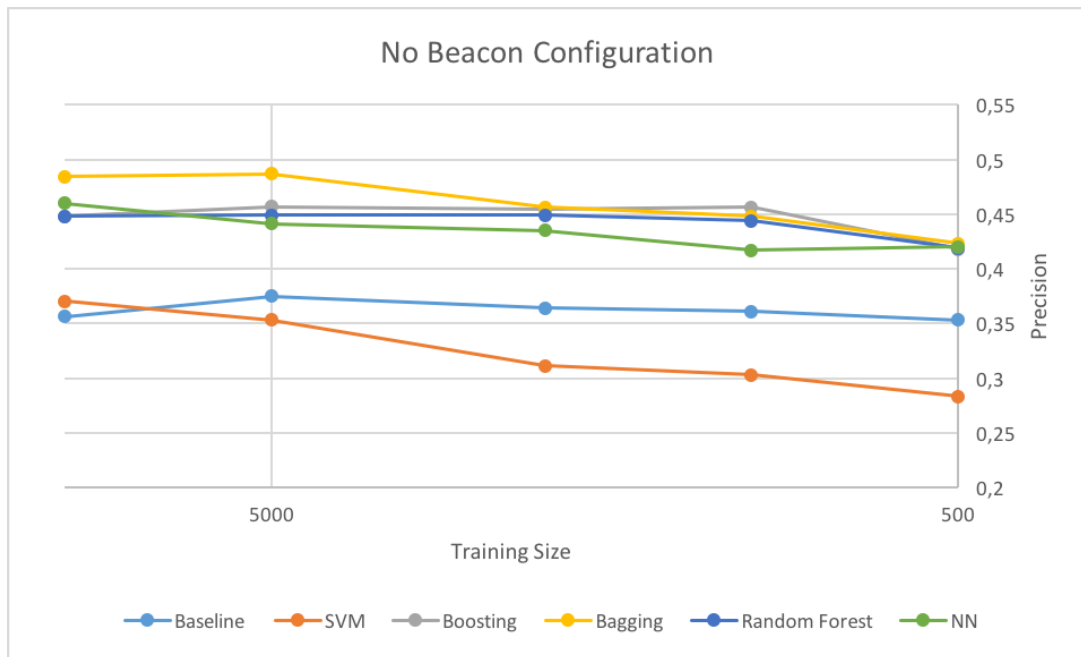


Figure 8: Precision evaluation of our selected models with different training size and with no beacons.

The first thing we can notice is that even if having a configuration with no noise improves the results, it doesn't by so much that we cannot work with noisy data.

Looking at Figure 7 and Figure 8 we can see different things: although as we could expect the more data we have, the better we predict, there appears to not be significant difference between 10000 and 5000 (we performed t-tests for both precision and recall using average and variance for ensemble methods with different training size, for example bagging 10000 with bagging 5000, not rejecting the null hypothesis, after confirming with Shapiro-Wilk that the

distribution seemed normal), and starting from 5000 going downwards the cost evaluations of most classifiers drop significantly.

In particular, the best classifier appears to be Bagging when we feed it with a lot of data (10000-5000, t-tests with the other ensemble methods resulted to be significantly different) and there is no significant difference among the three ensemble methods with lower data (we performed one-way ANOVA for both precision and recall evaluations after confirming normality of the distributions). As expected, the Baseline performs consistently with a little variety in the results. Also, SVM has the worst performance consistently among the not baseline classifiers for precision while keeping a reasonably good recall. Finally, NN performs better than the baseline with respect to precision, but it is terrible with recall.

Adding information from fixed position receivers, as we can see in Figure 9 and Figure 10, shows no significant improvement for our ensemble methods (we performed t-tests for each ensemble method with its correspondent model with beacons and in almost every case they resulted to be not significantly different. Bagging resulted to be different with 5000 samples, but it may be due to be using only 5 samples for each classifier), exception made with 500 samples where our models seemed to perform not even normally, probably due to being too little data to properly train our classifiers, a remarkable improvement on SVM, which appears to perform extremely better than the baseline with a lot of data, and a surprising worsening of the performance for NN, most likely caused by underfitting.

Summing things up:

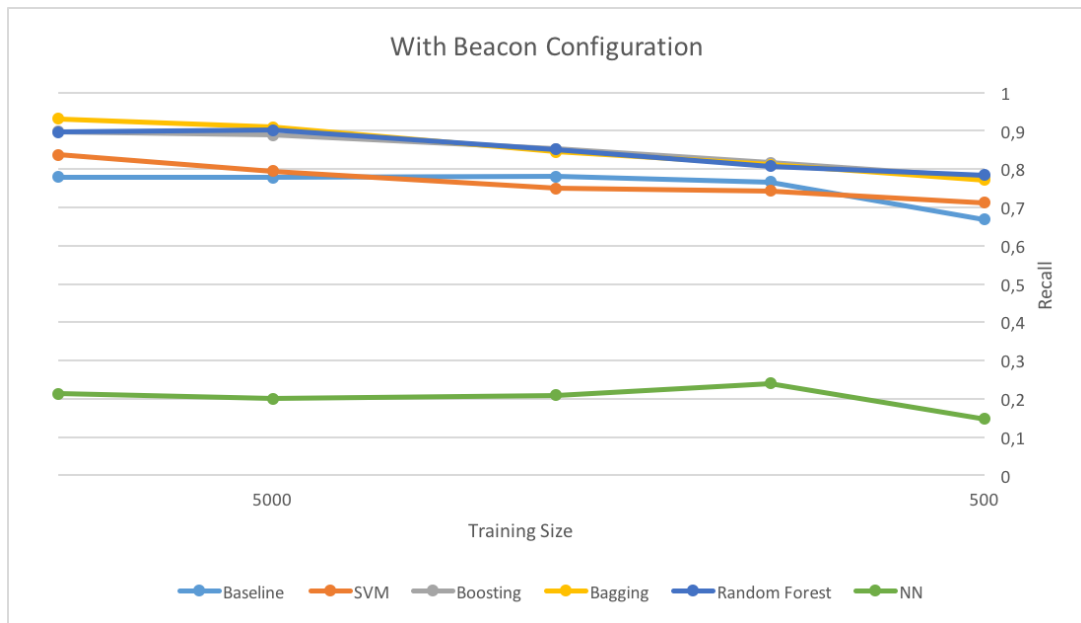


Figure 9: Recall evaluation of our selected models with different training size and with beacons.

- There does not appear to be an extreme advantage on using fixed position sensors for the top performing classifiers, with this little noise in the data.
- NN tuning of layers and number of neurons appears to be extremely difficult and time consuming to be used in an automatic way, for so many different configurations.
- Although having more data *does* improve the results, we cannot always use a big amount of data for computational constraints as well as for comparisons with real world labeling, thus we will use 2000 samples from now on, which still gives reasonably good performance while maintaining small enough computation time.

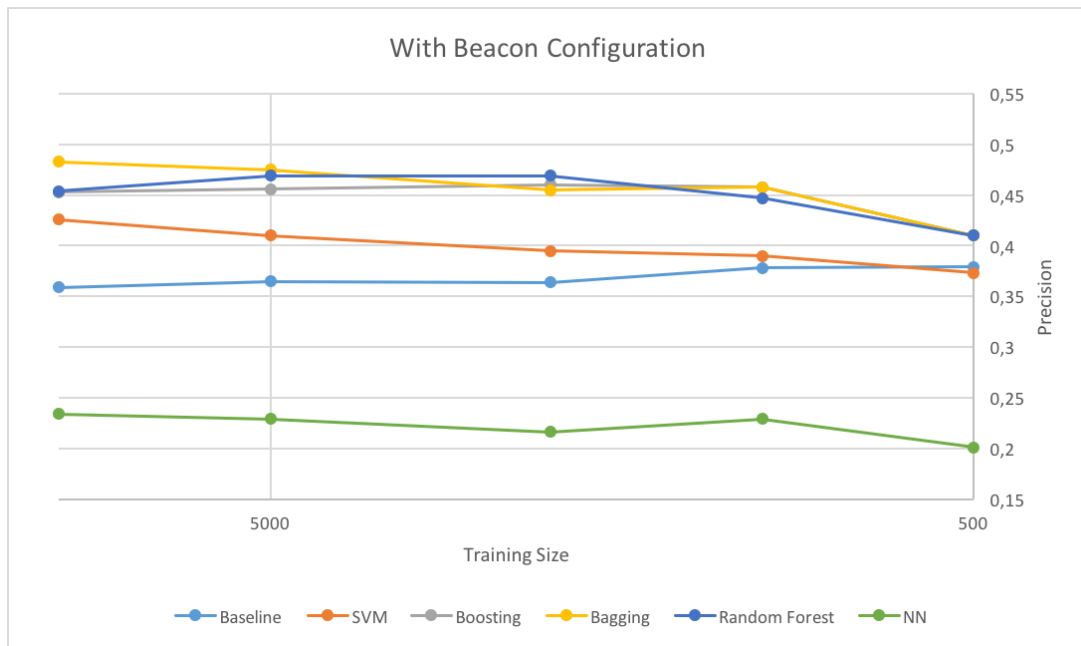


Figure 10: Precision evaluation of our selected models with different training size and with beacons.

5.2 Sensor Reliability

How reliable must sensors be to still have reasonable results? In this Section, we are interested in dropping the reliability of a transmitter to send a signal. If it doesn't, in that time frame no receiver receives it.

We will not use NNs anymore, as they appear to not be fit for the task, and we will decrease the reliability in a non linear fashion again.

We will only show our configuration with no beacons here. The reason is simple: adding beacons does not affect at all this type of errors, as beacons have only receivers, and when

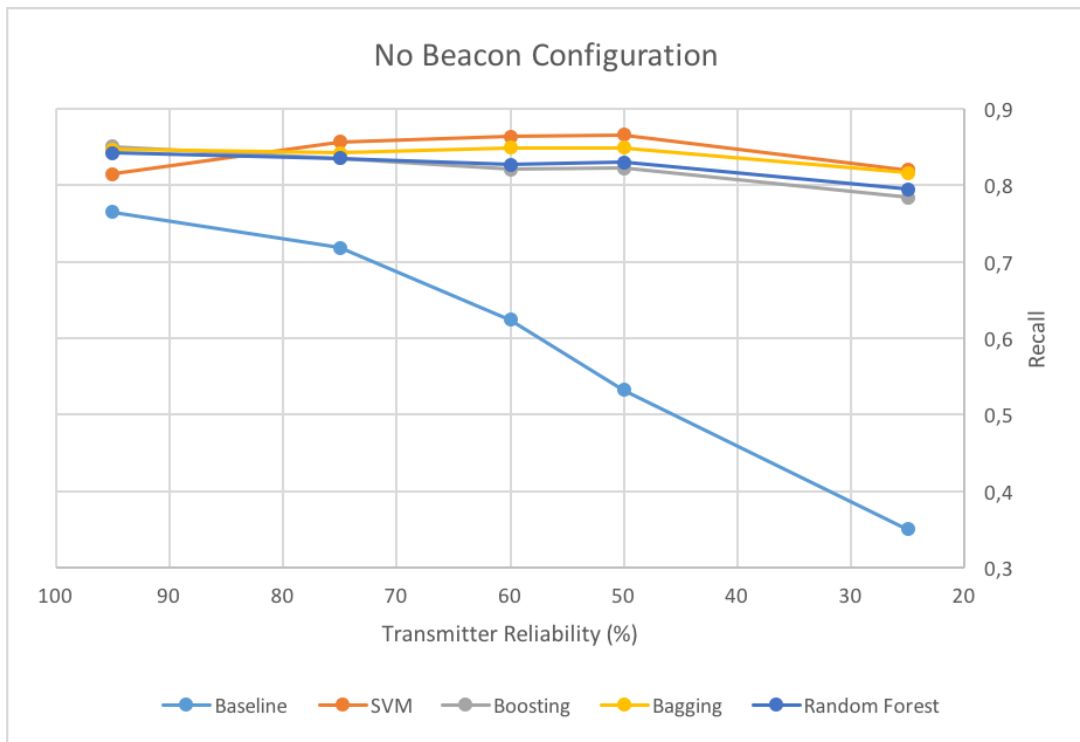


Figure 11: Recall evaluation of our selected models with different transmitter reliability and with no beacons.

transmitters fail they don't send *any* signal. Everything you will see is conceptually the same for the configuration with beacons, suggesting again we don't need beacons in this case, so we omitted it.

As expected, the performances drop for all classifiers. In particular, the precision is harmed significantly by this noise, as shown in Figure 12, for our ensemble methods, while both SVM and the baseline keep their (low) performance stable.

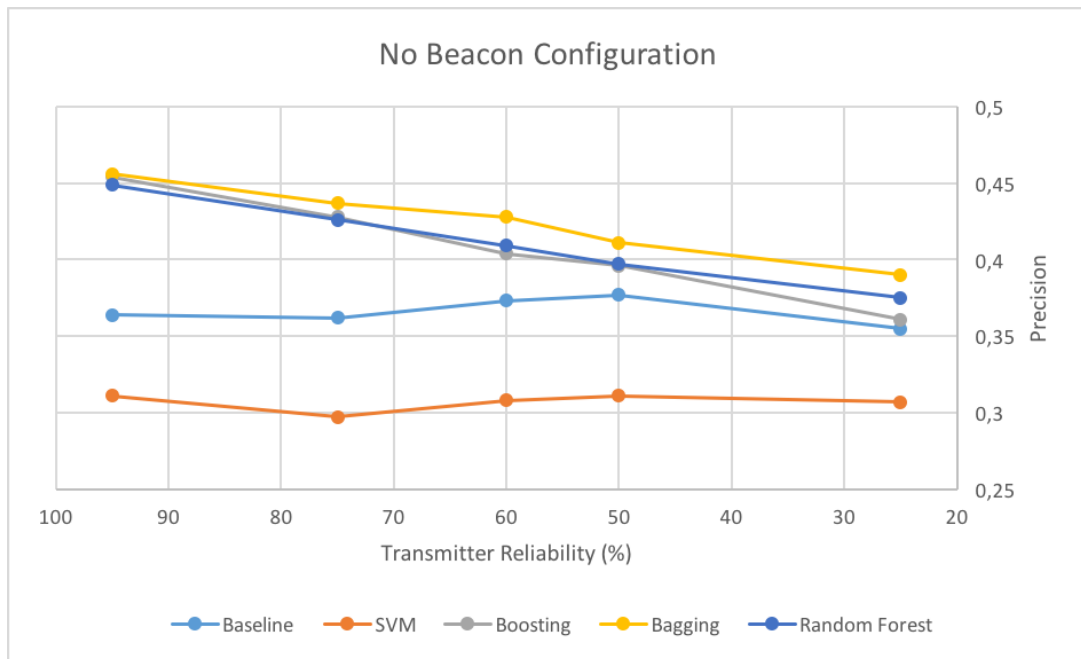


Figure 12: Precision evaluation of our selected models with different transmitter reliability and with no beacons.

Surprisingly, recall remains very high. In particular, the ensemble methods are able to make reasonable inferences even with extremely unreliable data, as seen in Figure 11, even if the precision falls behind 40%, maintaining a 80% recall.

Finally, our baseline's recall drops drastically, making it not usable at all.

5.3 Sensor Error

Transmitter and receiver errors are modeled in two different ways and have two different effects on our input data.

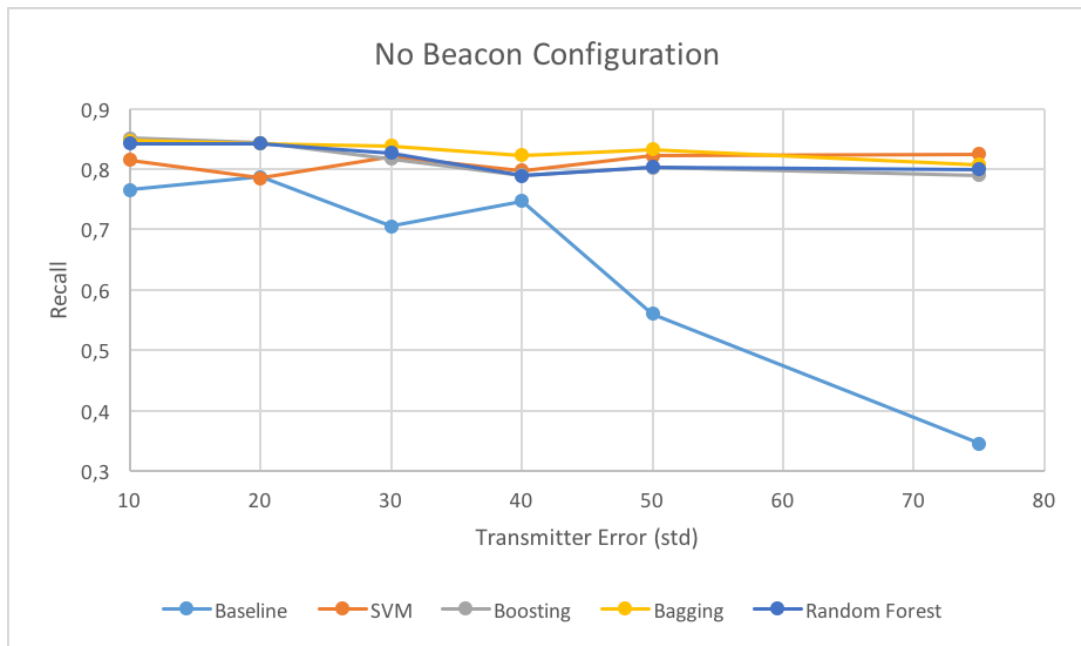


Figure 13: Recall evaluation of our selected models with different transmitter error and with no beacons.

We will first increase the noise on solely the transmitter signals. Second, we will analyze the effects of the noise in the receivers.

5.3.1 Transmitter Error

Again, being a type of error not regarding beacons, they don't help here and our models with and without beacons give the same results, so we omit the graphs with beacons here as well.

It appears that this kind of noise heavily impacts the performance of all our models. The baseline's performance in particular is terrible, while our models still keep respectable results. In particular, recall remains untouched (Figure 13), while precision drastically drops (Figure 14).

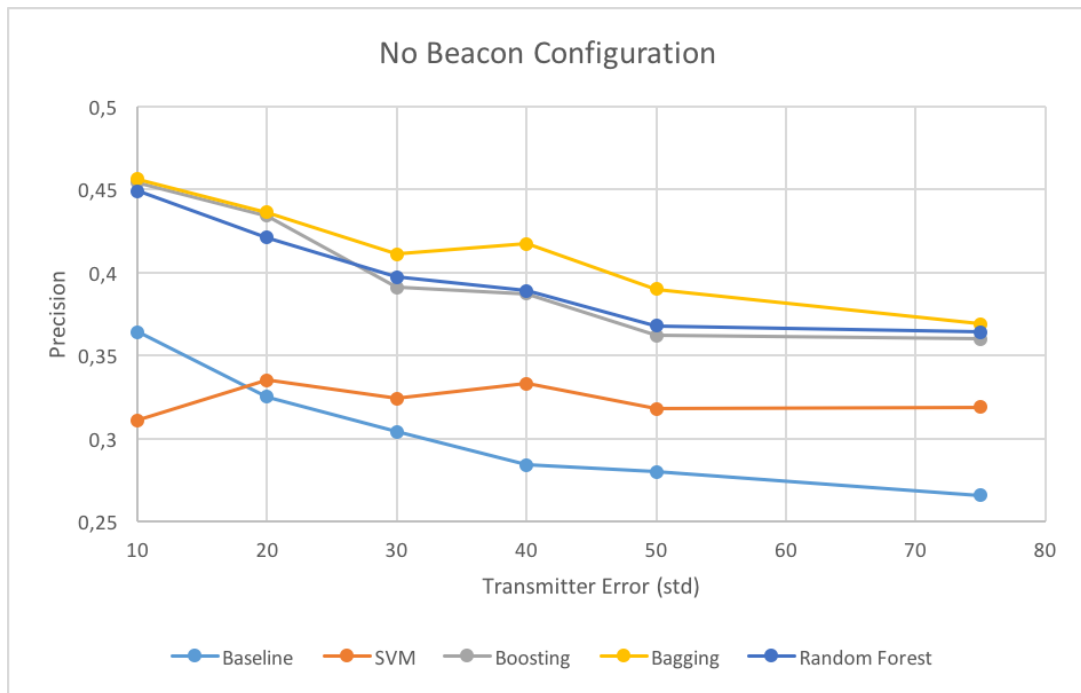


Figure 14: Precision evaluation of our selected models with different transmitter error and with no beacons.

5.3.2 Receiver Error

Receiver error can in principle be mitigated by adding beacons, so we will show both configurations:

With respect to the transmitter noise, this kind of noise impacts significantly less the performances of our classifiers. Recall still performs well (Figure 15) even if it decreases by a little bit, while precision decreases with a ‘lesser’ slope (Figure 16) with respect to other types of noise.

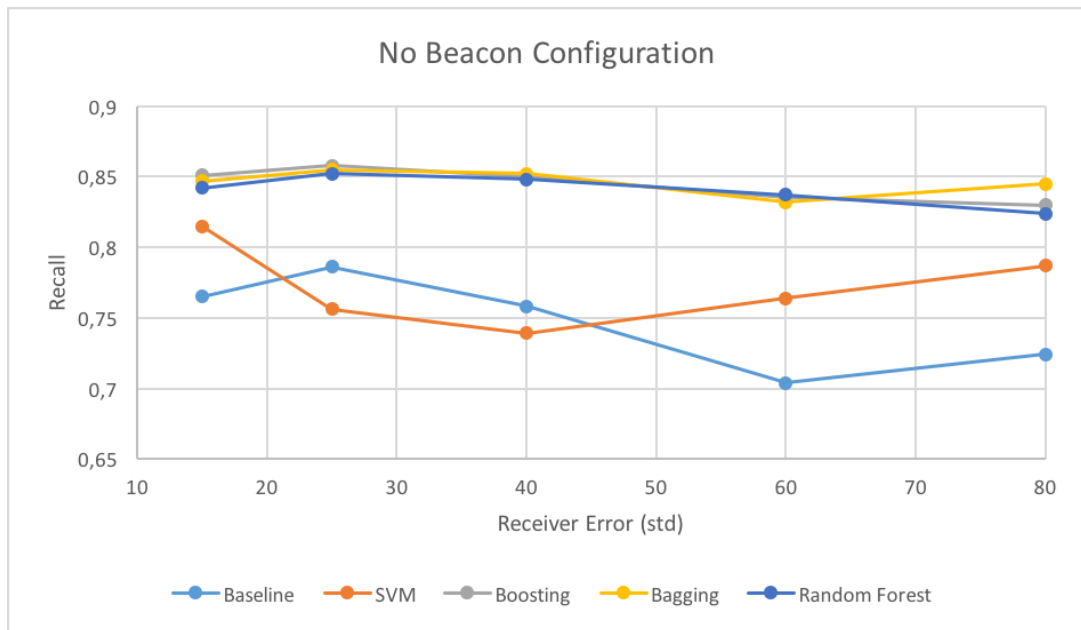


Figure 15: Recall evaluation of our selected models with different receiver error and with no beacons.

Being this the case, you can already imagine that beacons will not be of much help, as this noise was not a problem to begin with. Figure 17 and Figure 18 show just that: they don't seem to be of any impact. To be sure, we performed t-tests for each ensemble method for recall and precision, not resulting to be statistically different.

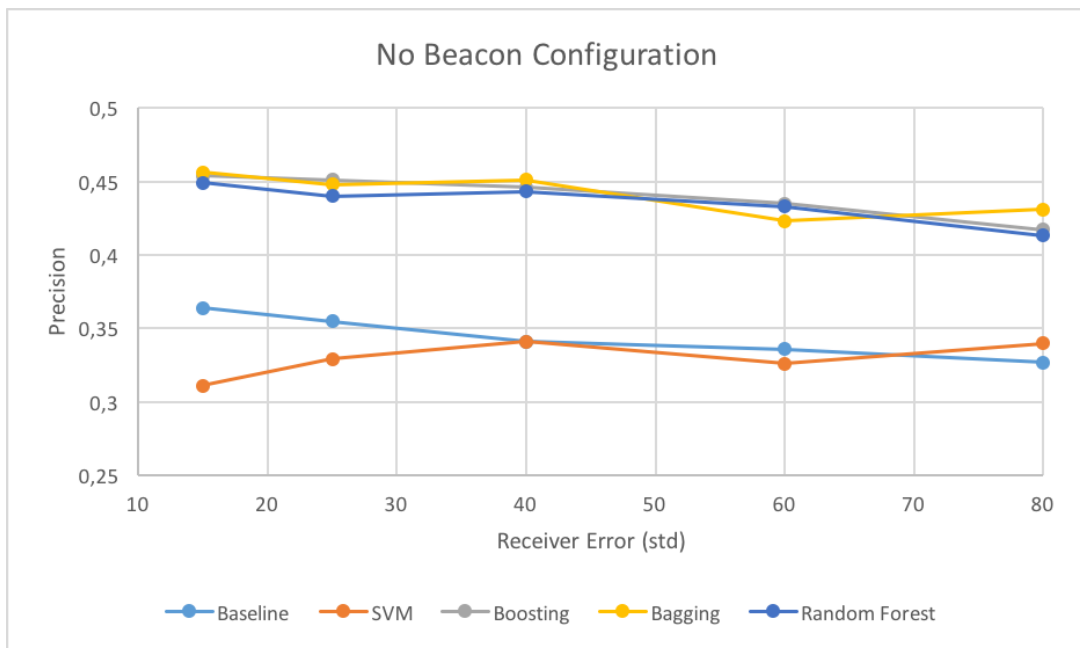


Figure 16: Precision evaluation of our selected models with different receiver error and with no beacons.

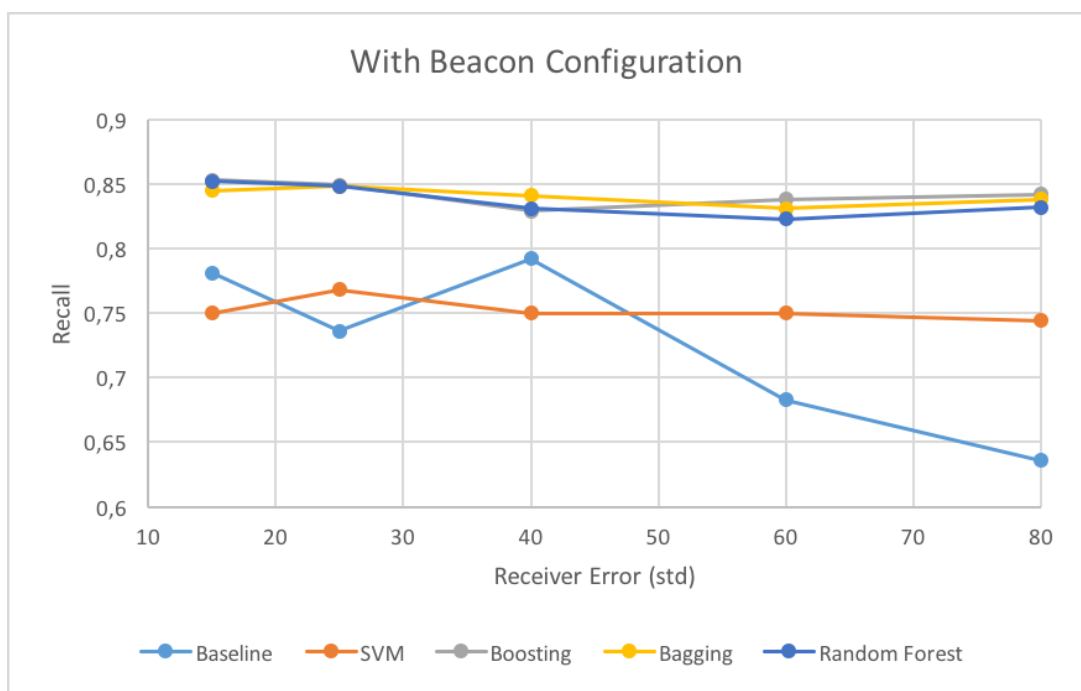


Figure 17: Recall evaluation of our selected models with different receiver error and with beacons.

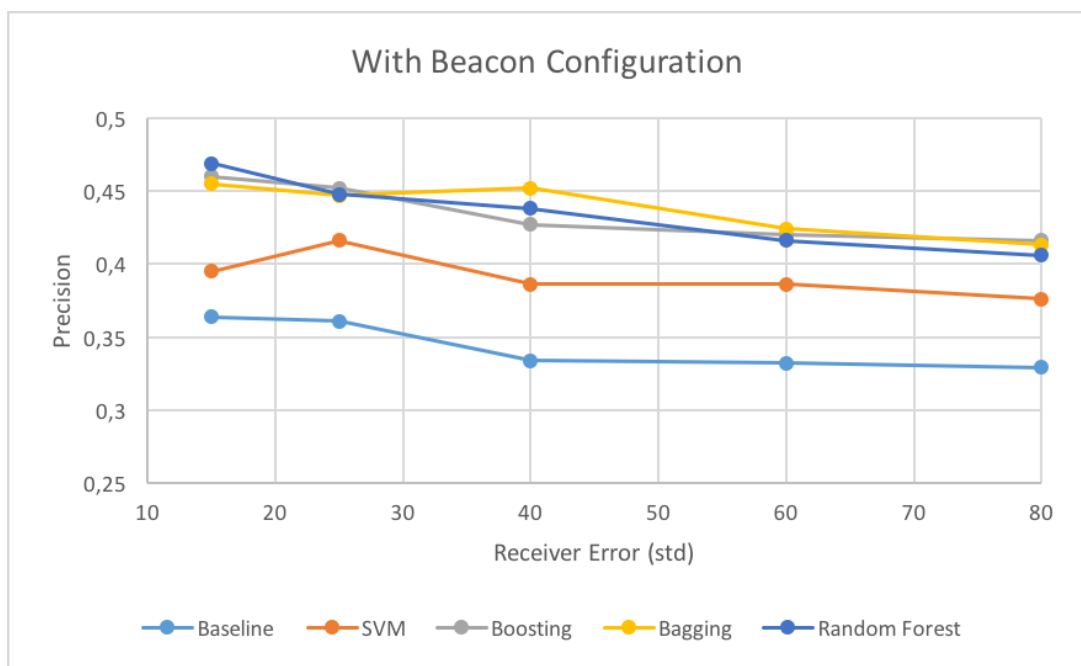


Figure 18: Precision evaluation of our selected models with different receiver error and with beacons.

5.4 Feature Relevance

We are interested in knowing what are the input features that impact the most on our models, to eventually trim down the input size.

We split our input features into:

- Absolute pairwise distances.
- Ranking pairwise distances.
- Speed of agents.

Exception made for the speed features, which are useless by themselves, we tried every combination of features with our standard configuration of 2000 training size, standard noise.

Being a feature analysis, it doesn't matter what configuration we use, in fact the results are the same for both with and without beacon configurations. Here we present the results for the configuration with on beacons, as we previously noticed it to be sufficient and adding beacons doesn't help.

Clearly, our baseline is unaffected by these features, because we use raw data for it. As we can see from Figure 19 and Figure 20, it appears that our models without speed features are worse than the baseline with respect to precision, and ranking distances are worse than the baseline even regarding recall. In particular, even when adding speed features, ranking distances by themselves give significantly worse results than the ones obtained with absolute distances alone (exception made for SVM w.r.t. recall, t-test for our models with ranking and absolute distance rejected the null hypothesis) but they are still very good at both precision

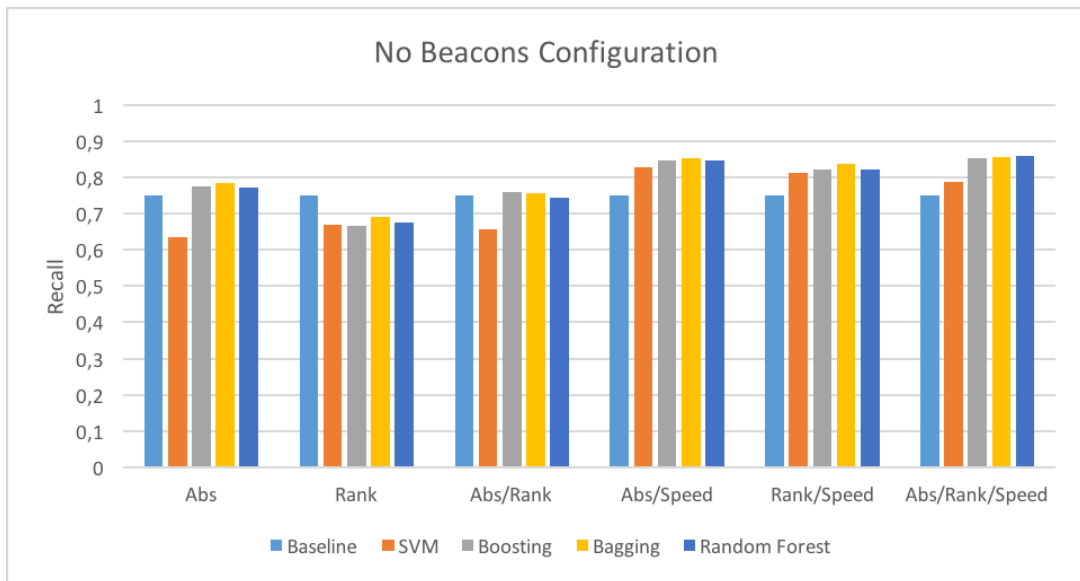


Figure 19: Recall evaluation of our selected models with different features and no beacons.

and recall, and the combination of the two does not improve significantly with respect to just having absolute distances for all models but SVM which worsens its results.

This result is interesting, and it is probably ought to the artificial labeling of our data. It is extremely reasonable to suppose that humans would label in a way much more similar to relative ranking distances than absolute ones, thus future work might want to see whether with different labels the situation might change.

It appears that our configuration doesn't overall require ranking distances (and beacons), while speed is extremely important.

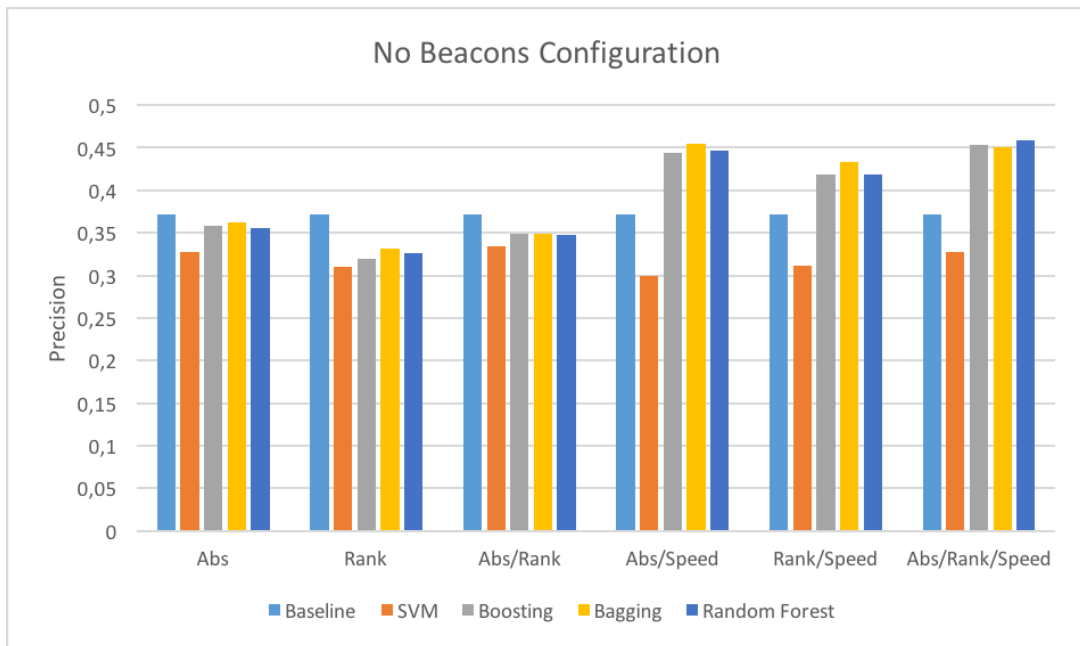


Figure 20: Precision evaluation of our selected models with different features and no beacons.

5.5 Adding Agents

We are interested in knowing what happens when we increase the number of agents in our fence. Up to now, we have always had 6 agents in our 5x5 meters squared environment. Now, we will increment this number. From now on, we will only use absolute distances and speeds in a configuration with no beacons, as it was shown to be more than enough in these configurations. Also, this task turned out to be extremely time consuming, thus we stopped after it took more than one day to compute a complete cycle (which we remember it to consist of 5 different runs, where we find the best model for each classifier with multiple training, then we train again and test each model).

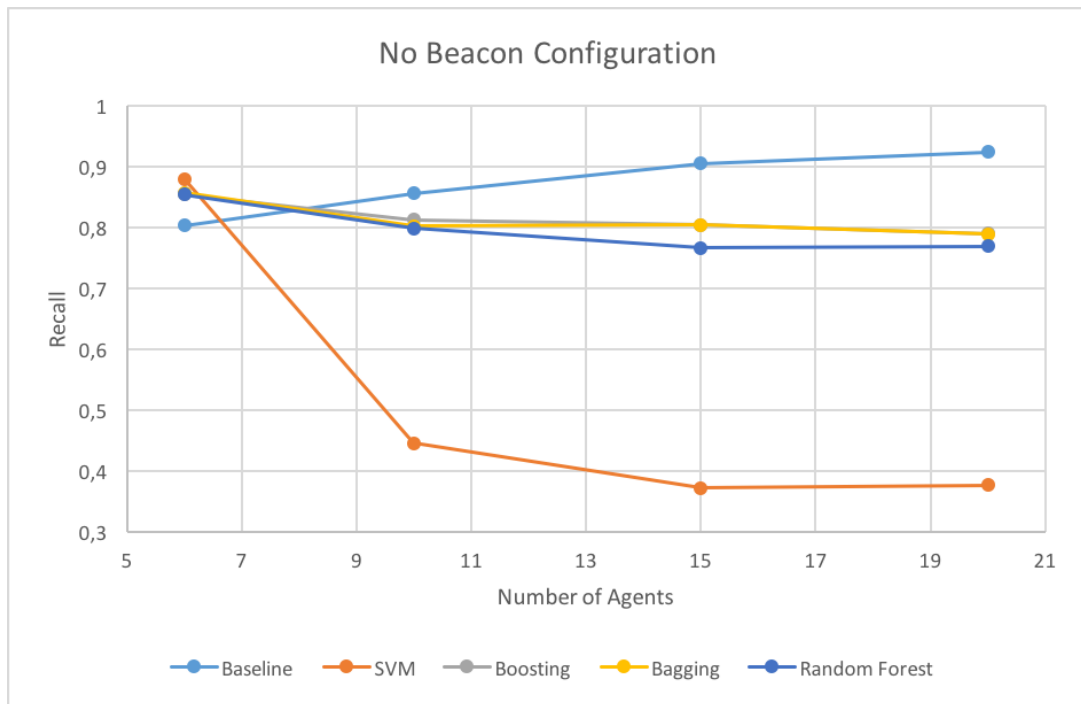


Figure 21: Recall evaluation of our selected models with different numbers of agents and with no beacons.

Figure 21 shows recall drops drastically for SVMs, a little for our ensemble methods and surprisingly it increases for our baseline. Figure 22 shows an increase of precision for all our classifiers, baseline included.

It appears that the more agents we add, the more likely we are to have an interaction, this explains the linear increase in performance for our baseline. Still, our ensemble methods perform consistently better than it.

We are curious to know what would happen in a larger environment, or with even more agents, or with a different agents behavior.

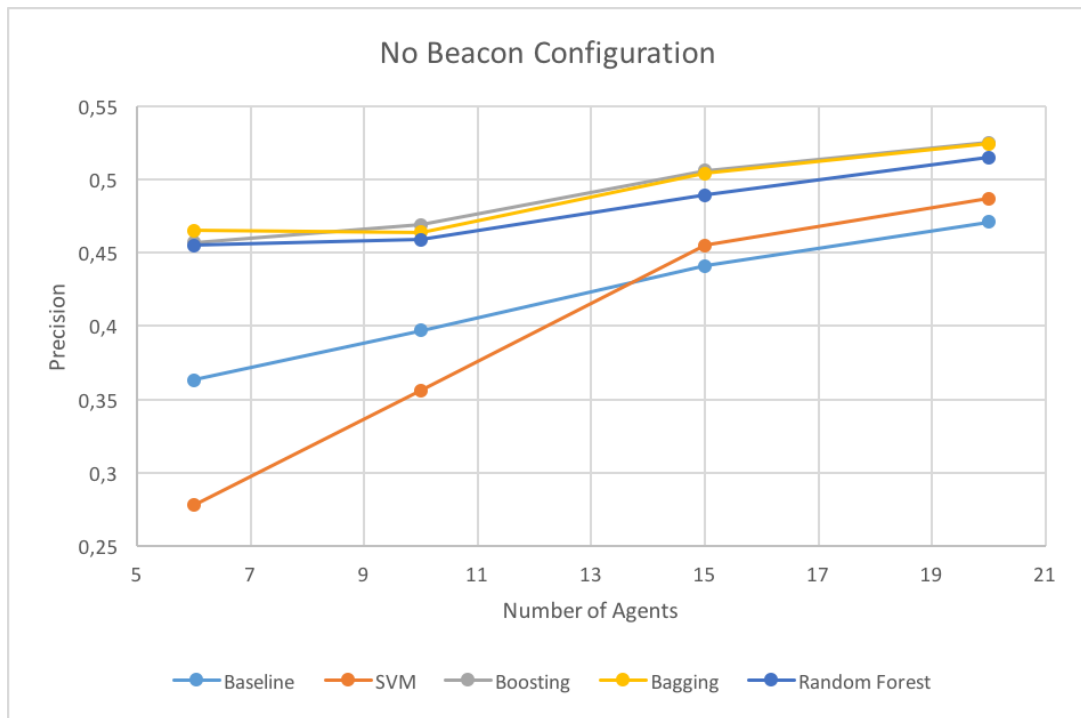


Figure 22: Precision evaluation of our selected models with different numbers of agents and with no beacons.

5.6 Decreasing Interactions

Probably the most critical parameter for our models to work is the likelihood of interactions between two close animals.

Being it a supervised learning approach which assumes differences among our animals, it generally needs a lot of data to work properly. When interactions become extremely rare, it starts to be a very big problem for our model to be trained properly.

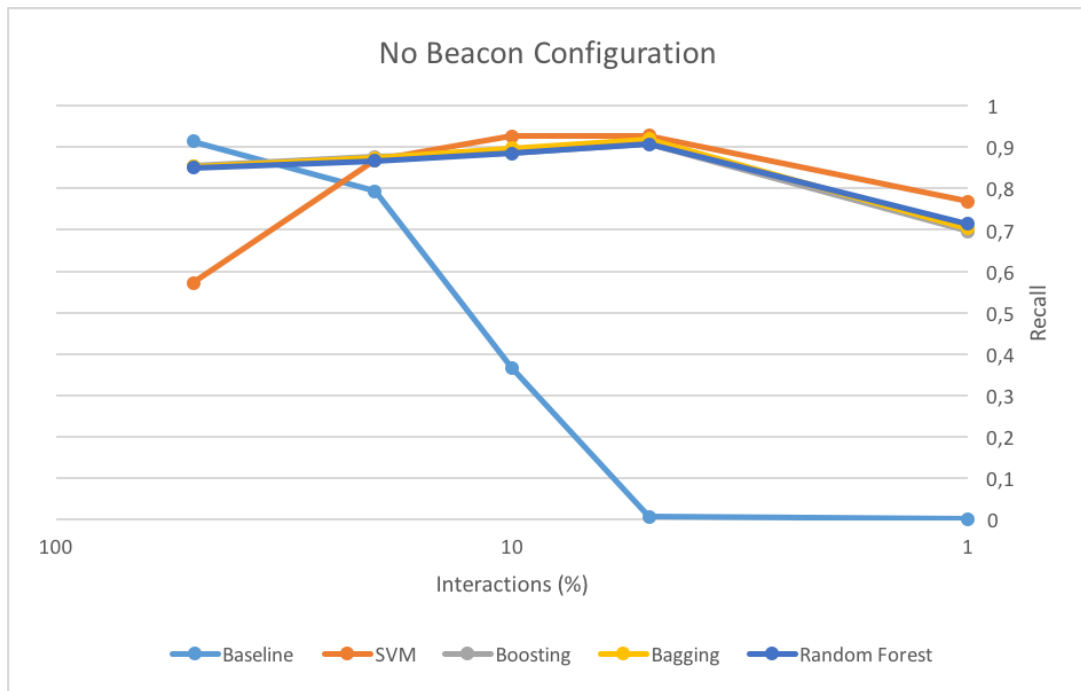


Figure 23: Recall evaluation of our selected models with different likelihood of interactions and with no beacons.

We are going to decrease our interaction likelihood and try to understand when our proposed models become unfit for the task, and different approaches should be considered.

Up to now, we have always used a 20% chance of interaction between two close animals. We will start with 50% and decrease it significantly, with a training size of 2000 timestamps, a cost matrix which considers false negatives three times more important than false positives and only using absolute distances and speeds, as before.

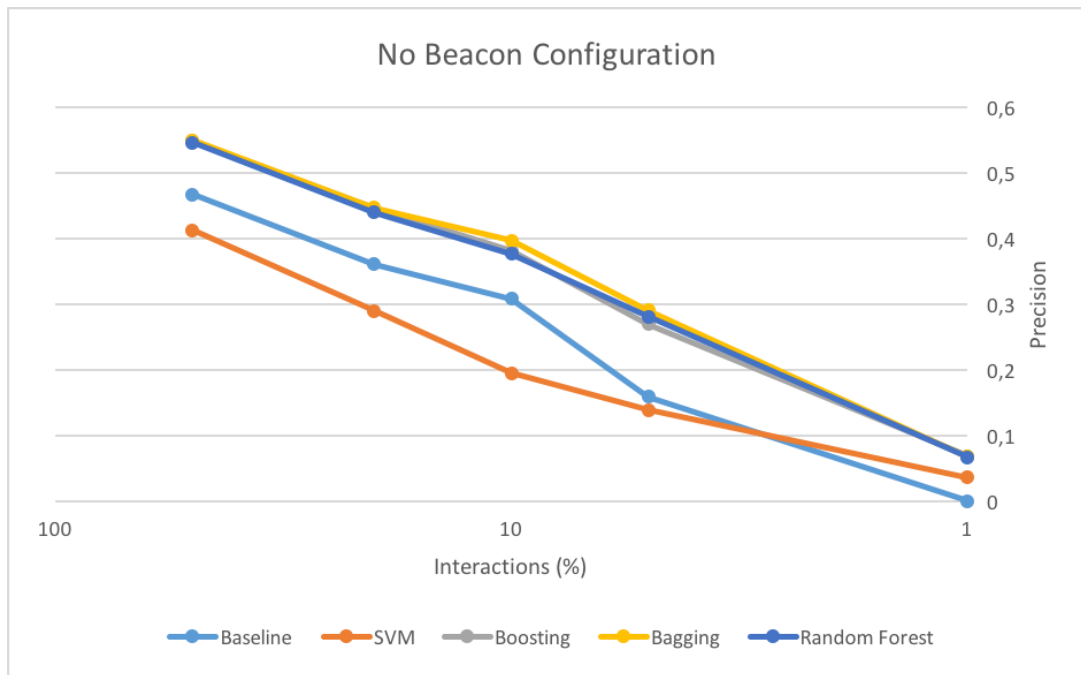


Figure 24: Precision evaluation of our selected models with different likelihood of interactions and with no beacons.

Figure 23 shows how the baseline quickly drops down to not ever predicting a positive result, while our models appear to hold a very high recall up to 5% interactions, to drastically drop their performance after.

Figure 24, however, shows how precision drops all the time we decrease the likelihood of interactions and even more when we reach 1%.

This was again predictable, because if the agents stay in the same small environment but interact less, its is extremely likely that just by chance more of their random movements look like an interaction, but it isn't. If we had a different type of interaction, in a bigger area, where

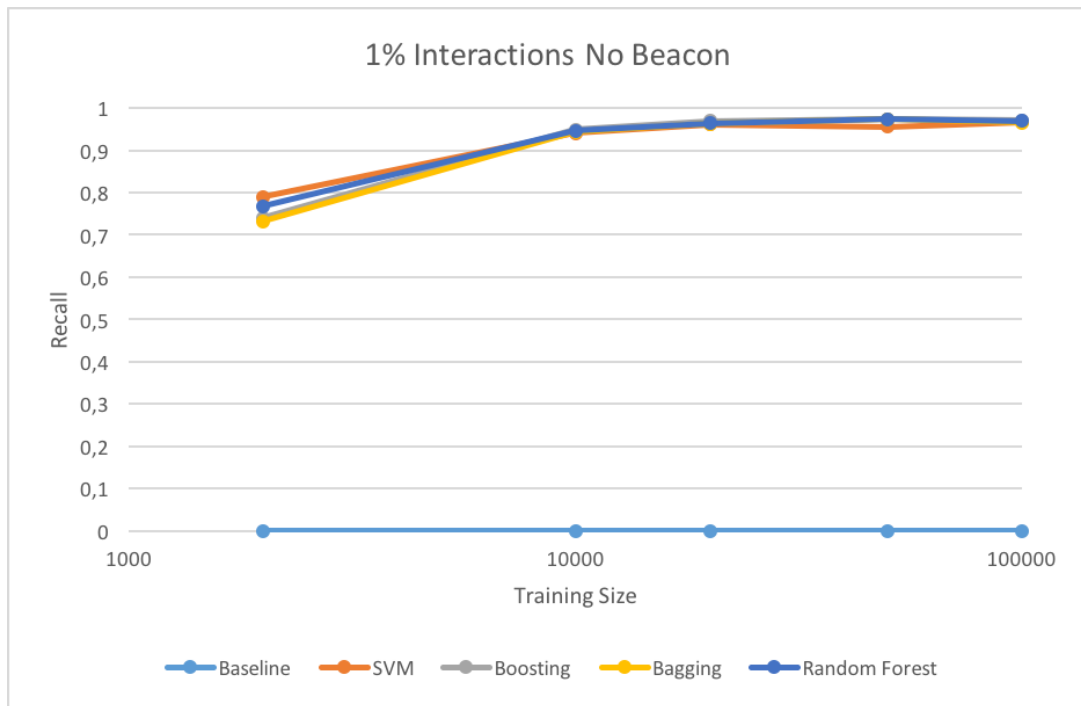


Figure 25: Recall evaluation of our selected models with different training size, 1% likelihood of interactions and no beacons.

being close to each other significantly increases the likelihood of an interaction, or with more specific accelerometer and orientation data, we expect our model to perform much better.

Still, we asked what would happen if we had more data. First of all, we modified the cost matrix to consider false negatives ten times more than false positives, then we significantly increased the training size to see if our models improved and by how much.

Figure 25 shows how recall increases until it stabilizes at 96% for all models but the baseline, which remains unable to predict a positive interaction. Figure 26 shows how precision grows *very slowly*, becoming excessively slow after 50000 samples.

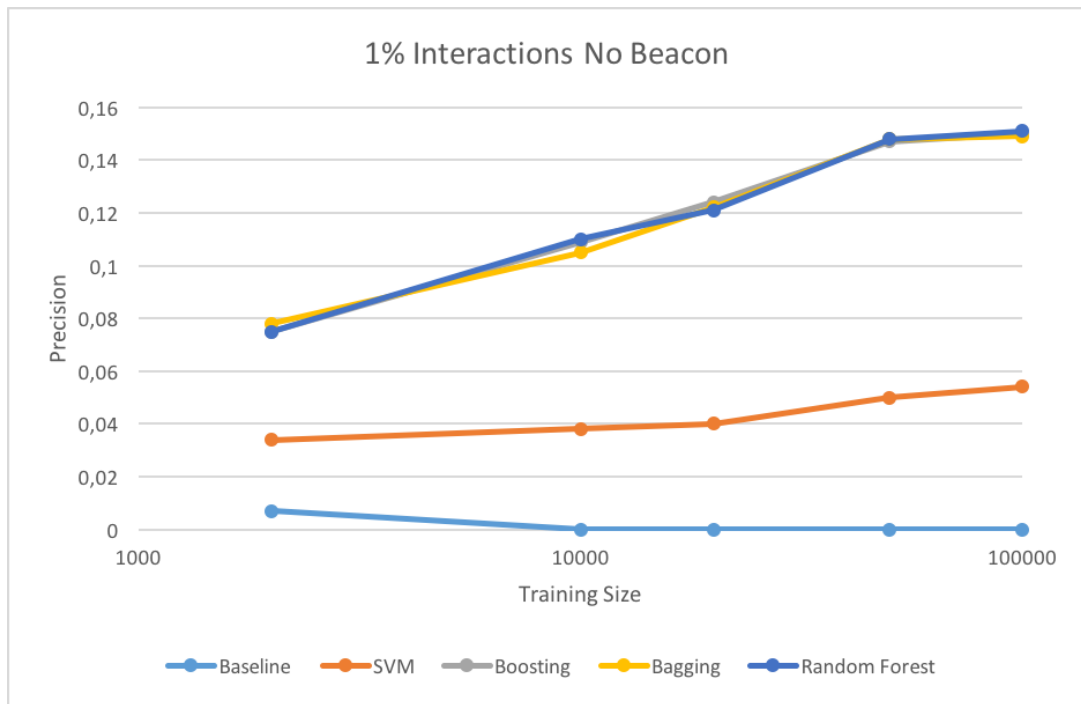


Figure 26: Precision evaluation of our selected models with different training size, 1% likelihood of interactions and no beacons.

This suggests us that for spotting this specific kinds of interactions, either this model might be too complex and we would need too much data, thus we should go with pairwise independent models, or it is too difficult to understand when an interaction does not occur without dropping the more important recall.

5.7 Families Comparison

Once we realized what our family of models without the use of any independence assumption can and cannot do, we can directly compare the top performing one with its counterpart of the other family: we took our Bagging classifier, with only absolute distances and speed, and

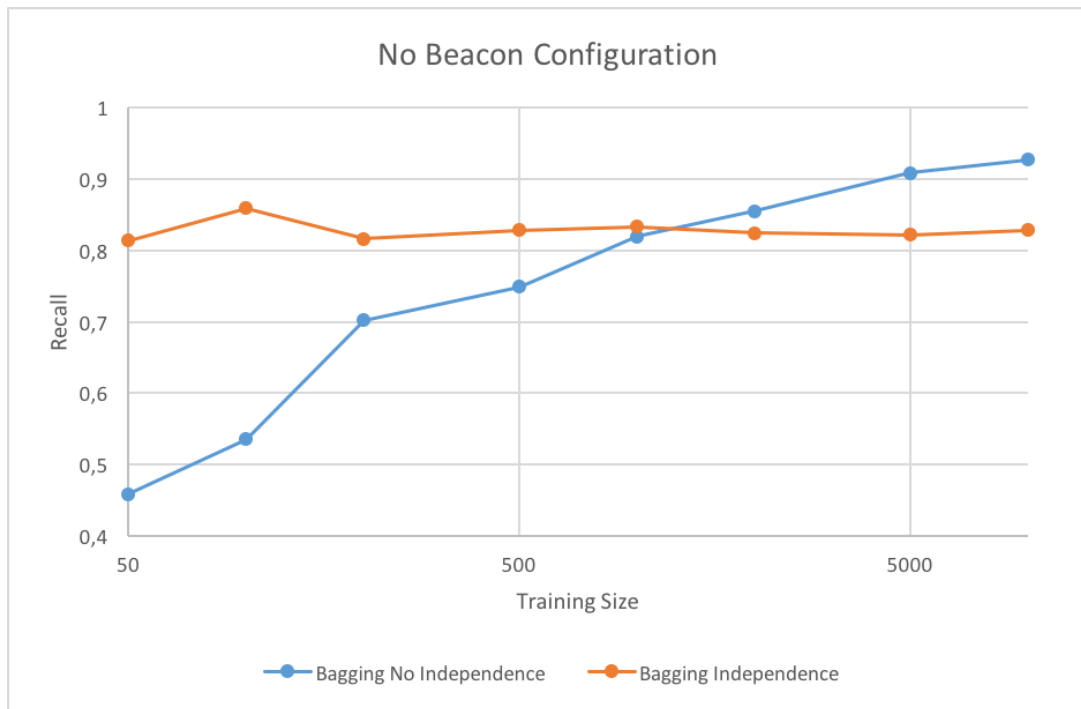


Figure 27: Recall evaluation of our Bagging models with and without assumptions with different training size and with no beacons.

with no beacons, and we compared it with the same bagging classifier, but with individual independence and pairwise independence assumptions.

5.7.1 Common Interactions Case

We first show their performances in our standard configuration of 20% interactions with varying training size. This time, however, having a model which performs well even with a little data, we started from 50 timestamps, up to again 10000.

As expected, our independence model performs astonishingly better than our other model when we have a little data. Figure 27 shows that while our assumption free model starts

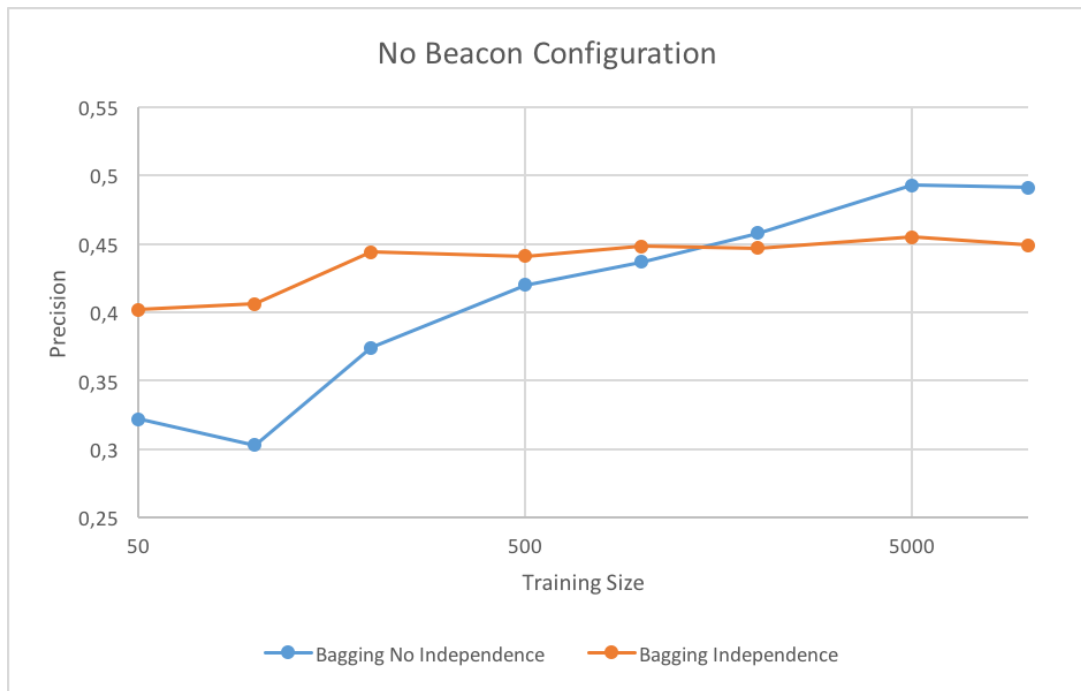


Figure 28: Precision evaluation of our Bagging models with and without assumptions with different training size and with no beacons.

with a terrible recall, to become extremely good after having more than 1000 timestamps, our independence model is consistent with more than 80% recall for every quantity of training size we feed it with.

Figure 28 shows the same trend for our assumption free model and a similar one for our independence one. This time, it seems that with a little data, even though it still is far better than its counterpart, it has still rooms for improvement, and it reaches its summit at 200 training size, which is anyway extremely low. We can notice that the turning point in this

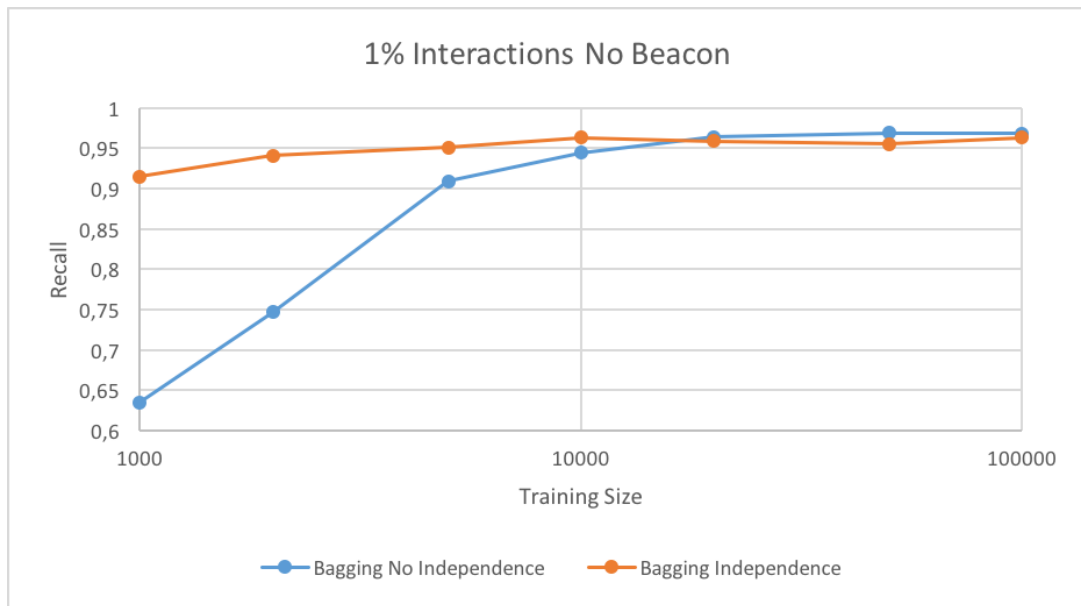


Figure 29: Recall evaluation of our Bagging models with and without assumptions with different training size and with no beacons with 1% interaction likelihood.

experiment turns out to be 1000 timestamps: if we have more data, we prefer our assumption free model, otherwise our independence model is far better.

5.7.2 Rare Interactions Case

We are extremely interested in what happens with rarer interactions. We noticed that our first family resulted to be struggling a lot with 1% interactions likelihood, and we didn't know what was the reason for it. We will try this configuration with both our families to give an insight about it.

The result is interesting: it appears that in this case our independence model performs better than our assumption free model even at 100000 training size.

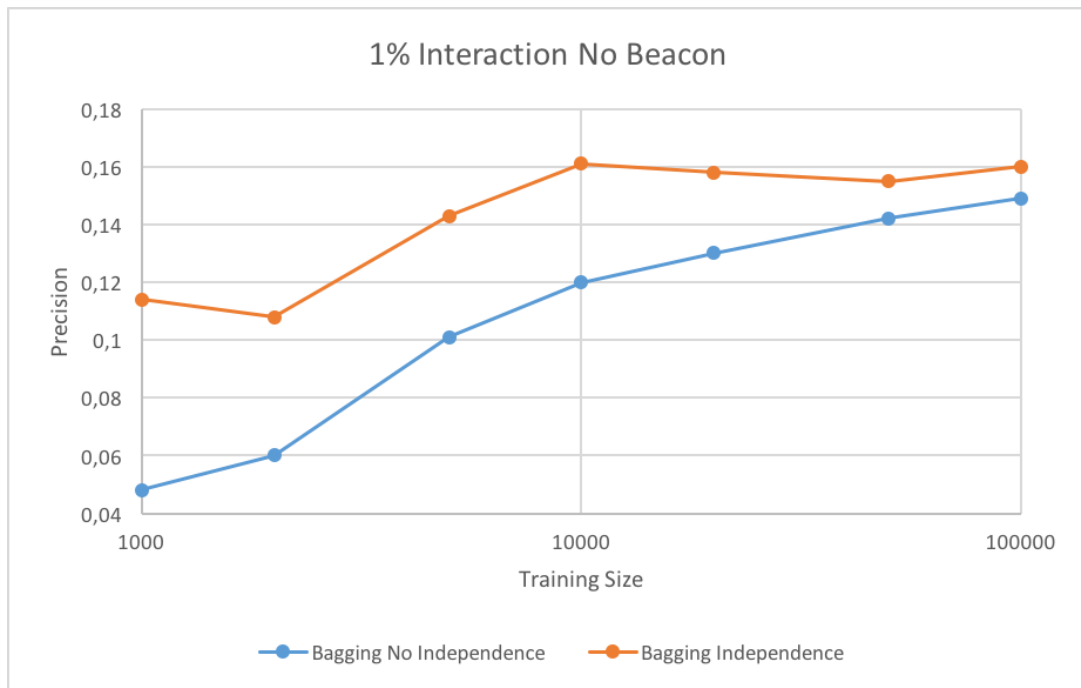


Figure 30: Precision evaluation of our Bagging models with and without assumptions with different training size and with no beacons with 1% interaction likelihood.

Figure 29 shows how both classifiers stabilize at 95-96% recall, but with our independence model starting with more than 90% w.r.t. less than 65% of its counterpart.

Figure 30 however shows two interesting things: the first is that, as mentioned before, our assumption free model never reaches its rival, suggesting that even more data would be needed to surpass it. Secondly, that after 10000 timestamps, our independence model stabilizes at 16% precision. This strongly suggests us that, even if our other model could in principle do a little better than this, the issue of its low precision doesn't come only from not having enough data,

but also because we don't either have enough specific sensors or the interaction was too oddly defined to begin with.

Nevertheless, it still shows that especially for rare interaction cases, we would have to use our independence model.

5.8 Case Study Conclusions

We performed sensitivity analysis on our case study with FSM agents in a virtual fence with and without fixed position receivers, exploiting a baseline and two different families of models.

The more training data we have, the better we classify. Reliability on transmitters is not critical for practical configurations, but their error is. Receivers error is sustainable in small amounts and in our configurations having fixed position beacons doesn't seem to be necessary, even with extremely noisy data.

With the types of interactions we created, ranking distances perform worse than absolute distances, but they are still very useful by themselves. However, we believe them being worse than absolute ones might be caused by our bias at creating interactions in that specific way, so it might be that more realistic agents or human labeling might turn this conclusion upside down.

Increasing the number of agents improved our performances, probably by making our predictions easier, but significantly increased the computational time needed to perform our tests.

Also, decreasing the likelihood of agents interactions extremely impacted our results, dropping the precision by an exponential amount, especially for our assumption free family. We compared our two families of models by using the top performing classifiers and we confirmed

that our independence family works very well even with a little data and that over normal conditions our assumption free model surpasses it, given enough data. We confirmed that for practical uses with low likelihood interactions our independence family is recommended and realized that in this case study, there is either a lack of specific sensors or an oddly defined type of interaction, which causes precision to remain low, when there are rare interactions.

CHAPTER 6

CONCLUSIONS AND FUTURE WORK

We introduced a new way of using proximity data extracted from RSSI values to infer pairwise interactions of animals by synthesizing such data and using it with our models and framework. We created different families of models for a supervised learning approach: assumptions free and independence assumption families. We created a framework to perform extensive sensitivity analysis for calibrating any sensor system for inferring biological interactions which gives us the best model to use given any type of sensor data.

Our models work with arbitrary sensor data (GPS data can be used as well, of course it is still recommended to give distances and not positions as inputs) and can use context variables such as time of the day, season, specific places and so on.

Our framework for sensitivity analysis can be used to give guidelines for deploying sensors for a real configuration as well as suggesting the amount of training data required, and can give protocols for models and parameters selections.

Actual suggestions we were able to give to biologists are: we showed evidence supporting the thesis that ranking distances are useful and usable, that BLE sensors can be used in the field, that fixed position beacons are not necessary when we are interested in dyadic interactions, at least when we can have pairwise distances by applying them to animals, that accelerometer data is vital to spot specific types of interactions. We also discussed about when such models can be used and for what types of interactions. Finally, we gave some guidelines to how much

data we would need to have labeled for our models to work, with respect to the likelihood of interactions.

Future work can be done in many areas: we definitely need to try our models with human labeled data to see how it performs with real configurations.

We can add information of orientation of animals, to be able to give an idea if an animal is looking at another kin or not, which might significantly increase the accuracy of most human labeled and better synthesized models.

We can exploit Active Learning [34] to manually aid our model where it doesn't perform well, in our case, to try to increase the precision, trying to understand when it isn't able to spot a false positive and focus on labelling the types of interactions that are classified with the most errors, effectively decreasing the amount of data to label.

Finally, we might also be interested in knowing the absolute positions of our animals given our sensor, to see if it is possible to accurately triangulate their positions in a closed environment.

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